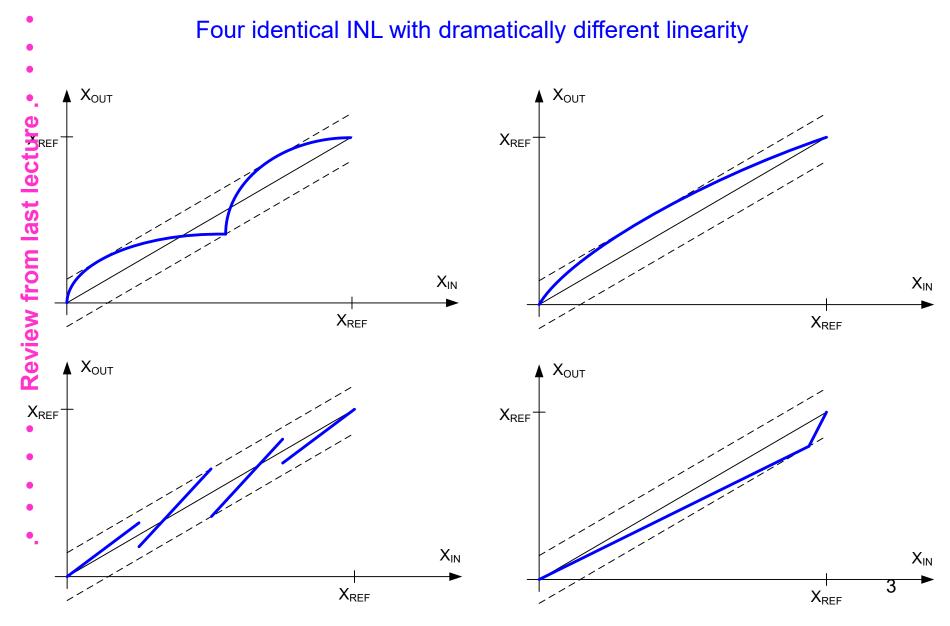
EE 435

Lecture 29

Data Converters

- Spectral Performance
 - Windowing
- Quantization Noise

INL Often Not a Good Measure of Linearity



• • • • • Review from last lecture .• • • • •

Distortion Analysis

How are spectral components determined?

By integral

$$A_{k} = \frac{1}{\omega T} \left(\int_{t_{1}}^{t_{1}+T} f(t) e^{-jk\omega t} dt + \int_{t_{1}}^{t_{1}+T} f(t) e^{jk\omega t} dt \right)$$
or

$$a_{k} = \frac{2}{\omega T} \int_{t_{1}}^{t_{1}+T} f(t) \sin(kt\omega) dt \qquad b_{k} = \frac{2}{\omega T} \int_{t_{1}}^{t_{1}+T} f(t) \cos(kt\omega) dt$$

Integral is very time consuming, particularly if large number of components are required

By DFT (with some restrictions that will be discussed)

By FFT (special computational method for obtaining DFT)

Why is this a Key Theorem? $x(t) = A_0 + \sum_{k=1}^{h-1} A_k \sin(k\omega t + \theta_k)$ THEOREM: Consider a periodic signal with period T=1/f and sampling period $T_s = 1/f_s$. If N_P is an integer, x(t) is band limited to f_{MAX} , and $f_s > 2f_{max}$, then $\left|A_{m}\right| = \frac{2}{N} \left|X(mN_{P}+1)\right|$ $0 \le m \le h - 1$ and X(k) = 0 for all k not defined above where $\langle X(k) \rangle_{k=0}^{N-1}$ is the DFT of the sequence $\langle X(kT_s) \rangle_{k=0}^{N-1}$

<A_k> are the Fourier Series Coefficients, N=number of samples, N_P is the number of periods, and $h = Int \left(\frac{f_{MAX}}{f} - \frac{1}{N_{P}} \right)$

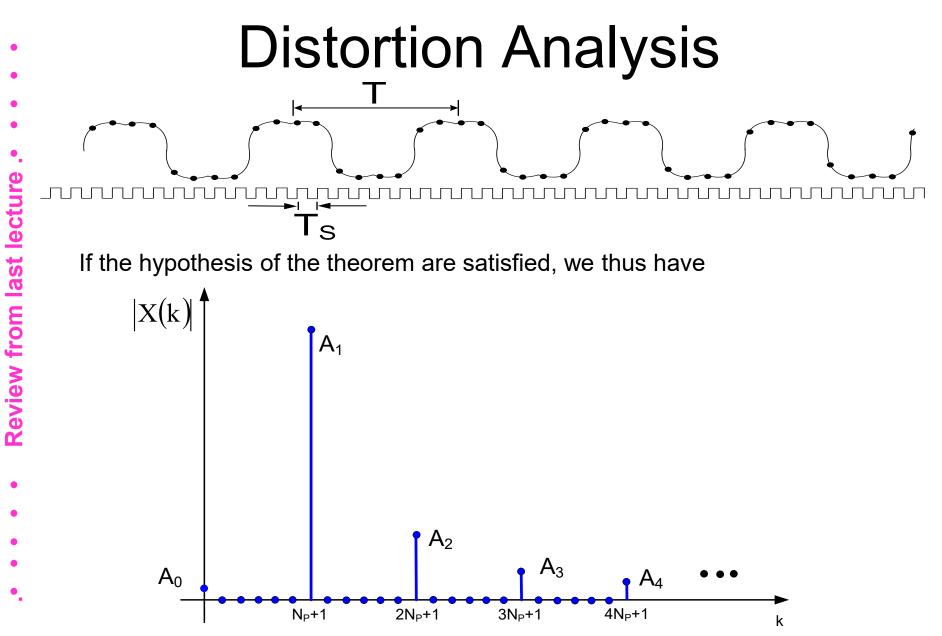
- DFT requires dramatically less computation time than the integrals for obtaining Fourier Series coefficients
- Can easily determine the sampling rate (often termed the Nyquist rate) to satisfy the band limited part of the theorem

5

• If "signal" is output of a system (e.g. ADC or DAC), f_{MAX} is independent of f

How is this theorem abused? $\mathbf{x}(t) = \mathbf{A}_{0} + \sum_{k=1}^{h-1} \mathbf{A}_{k} \sin(k\omega t + \mathbf{\theta}_{k})$ Ts THEOREM: Consider a periodic signal with period T=1/f and sampling period $T_s = 1/f_s$. If N_P is an integer, x(t) is band limited to f_{MAX} , and $f_s > 2f_{max}$, **Review from last lecture** then $|A_m| = \frac{2}{N} |X(mN_P + 1)|$ $0 \le m \le h - 1$ and X(k) = 0 for all k not defined above where $\langle X(k) \rangle_{k=0}^{N-1}$ is the DFT of the sequence $\langle x(kT_s) \rangle_{k=0}^{N-1}$

- <A_k> are the Fourier Series Coefficients, N=number of samples, N_P is the number of periods, and $h = Int \left(\frac{f_{MAX}}{f} \frac{1}{N_P} \right)$
- Much evidence of engineers attempting to use the theorem when N_P is not an integer
- Challenging to have N_P an integer in practical applications
- Dramatic errors can result if there are not exactly an integer number of 6 periods in the sampling window



Considerations for Spectral Characterization

Tool Validation

•DFT Length and NP

Importance of Satisfying Hypothesis

•Windowing

Considerations for Spectral Characterization

- Tool Validation
- DFT Length and NP
- Importance of Satisfying Hypothesis
 - NP is an integer
 - Band-limited excitation
- Windowing

Considerations for Spectral Characterization

- Tool Validation
- DFT Length and NP
- Importance of Satisfying Hypothesis
 - NP is an integer
 - Band-limited excitation
- Windowing

DFT Examples

Recall the theorem that provided for the relationship between the DFT terms and the Fourier Series Coefficients required

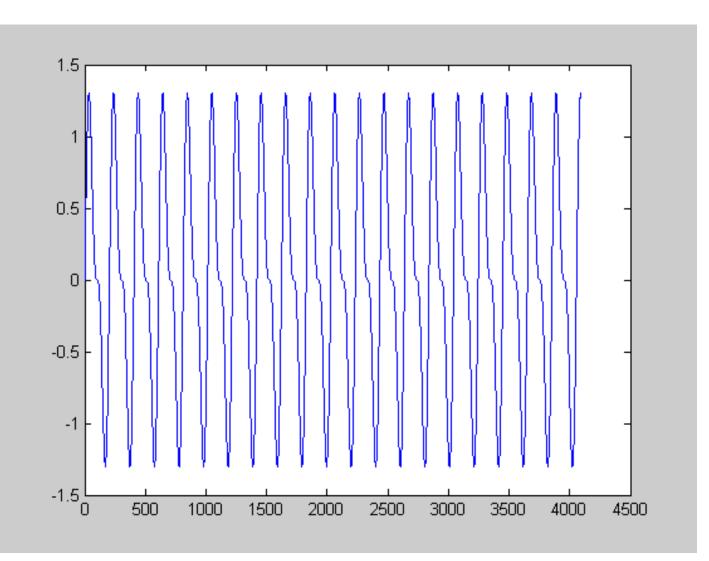
1. The sampling window must be an integral number of periods 2. $N > \frac{2 f_{max}}{f_{SIGNAL}} N_{P}$

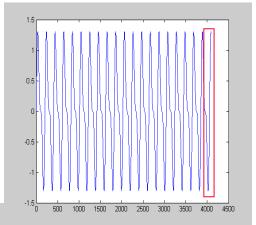
Example

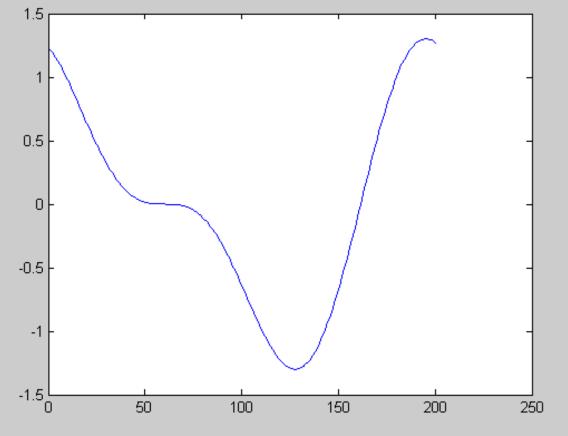
WLOG assume f_{SIG} =50Hz $V_{IN} = sin(\omega t) + 0.5 sin(2\omega t)$ $\omega = 2\pi f_{SIG}$

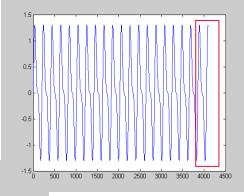
Consider N_P =20.2 N=4096

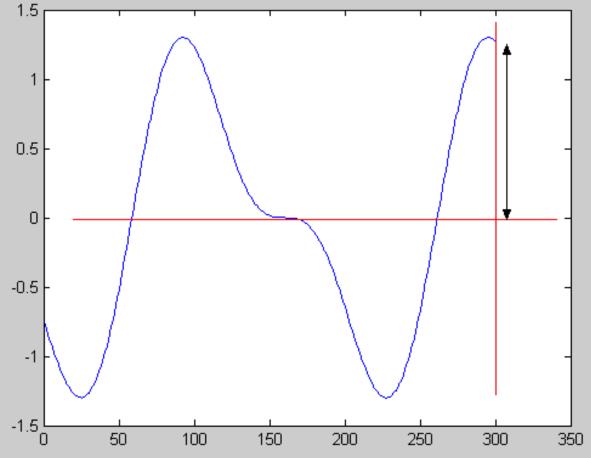
Recall 20log₁₀(0.5)=-6.0205999

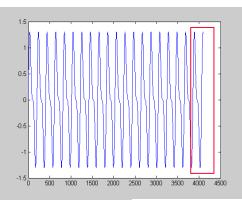


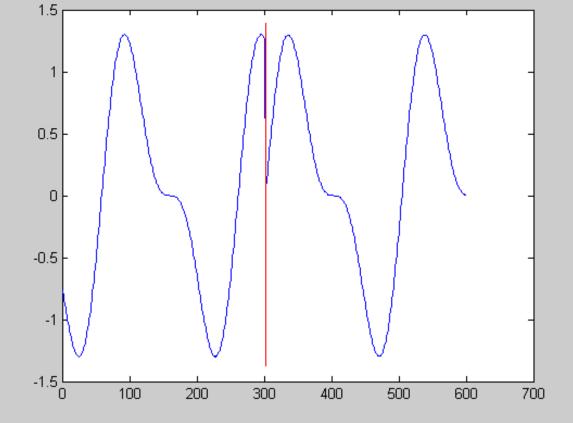




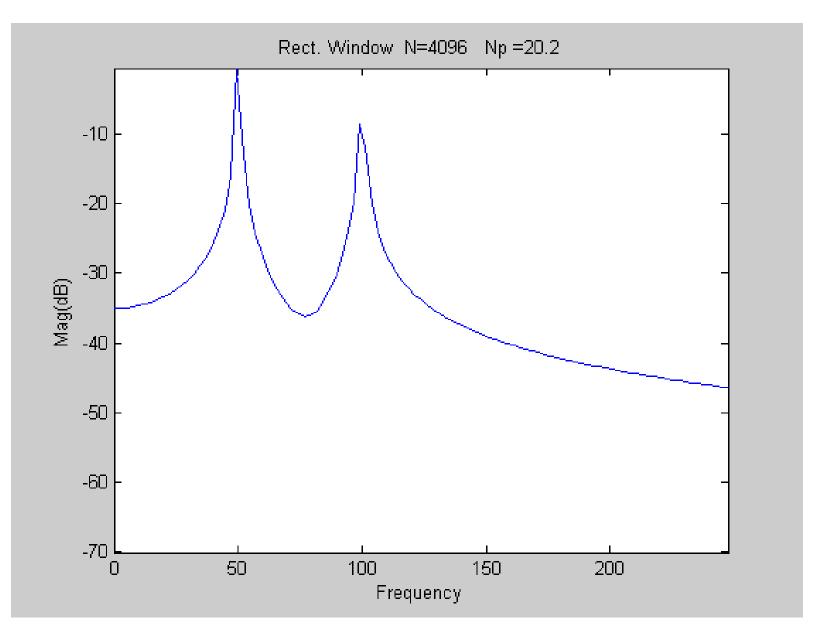








Spectral Response



Fundamental will appear at position 1+Np = 21

Columns 1 through 7

-35.0366 -35.0125 -34.9400 -34.8182 -34.6458 -34.4208 -34.1403

Columns 8 through 14

-33.8005 -33.3963 -32.9206 -32.3642 -31.7144 -30.9535 -30.0563

Columns 15 through 21

-28.9855 -27.6830 -26.0523 -23.9155 -20.8888 -15.8561 **-0.5309**

Columns 22 through 28

-12.8167 -20.1124 -24.2085 -27.1229 -29.4104 -31.2957 -32.8782

Columns 29 through 35

-34.1902 -35.2163 -35.9043 -36.1838 -35.9965 -35.3255 -34.1946

Note there is a dramatic increase in the noise floor and a significant change in and spreading of the fundamental!!

kth harmonic will appear at position 1+k•Np

Columns 36 through 42 -32.6350 -30.6397 -28.1125 -24.7689 -19.7626 -8.5639 -11.7825 Columns 43 through 49 -20.0158 -23.9648 -26.5412 -28.4370 -29.9279 -31.1519 -32.1874 Columns 50 through 56 -33.0833 -33.8720 -34.5759 -35.2113 -35.7902 -36.3218 -36.8133 Columns 57 through 63 -37.2703 -37.6974 -38.0984 -38.4762 -38.8336 -39.1725 -39.4949 Columns 64 through 70

-39.8024 -40.0963 -40.3778 -40.6479 -40.9076 -41.1576 -41.3987

kth harmonic will appear at position 1+k•Np

Columns 36 through 42 -32.6350 -30.6397 -28.1125 -24.7689 -19.7626 -8.5639 -11.7825 Columns 43 through 49 -20.0158 -23.9648 -26.5412 -28.4370 -29.9279 -31.1519 -32.1874 Columns 50 through 56 -33.0833 -33.8720 -34.5759 -35.2113 -35.7902 -36.3218 -36.8133 Columns 57 through 63 -37.2703 -37.6974 -38.0984 -38.4762 -38.8336 -39.1725 -39.4949 Columns 64 through 70

-39.8024 -40.0963 -40.3778 -40.6479 -40.9076 -41.1576 -41.3987

Observations

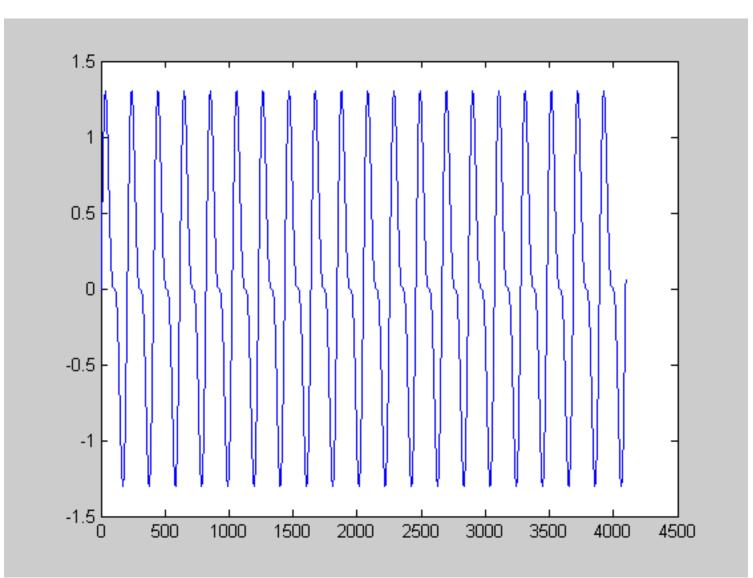
- Modest change in sampling window of 0.2 out of 20 periods (1%) results in a big error in both fundamental and harmonic
- More importantly, dramatic raise in the noise floor !!! (from over -300dB to only -12dB)

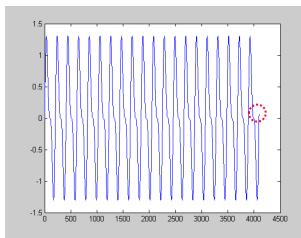
Example

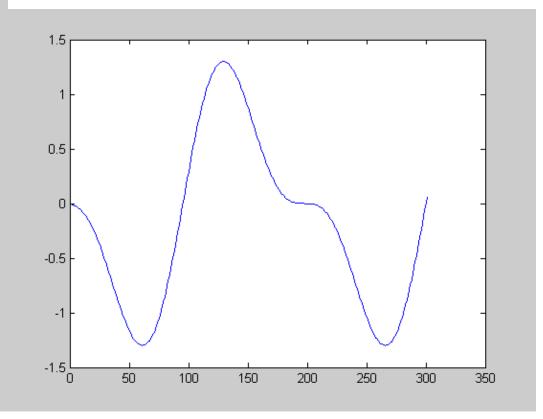
WLOG assume f_{SIG} =50Hz $V_{IN} = sin(\omega t) + 0.5 sin(2\omega t)$ $\omega = 2\pi f_{SIG}$

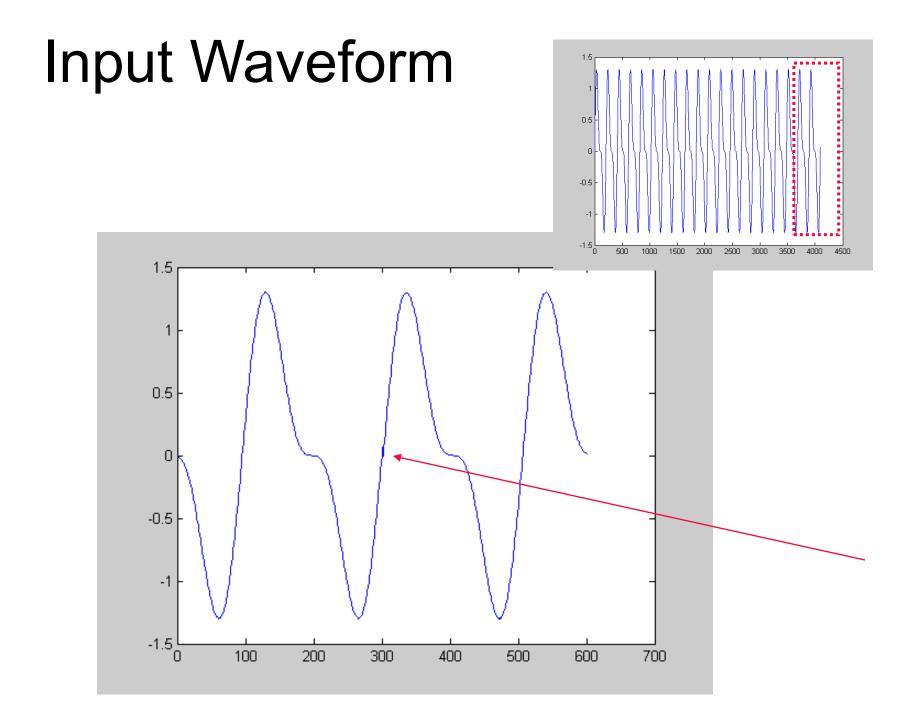
Consider N_P=20.01 N=4096

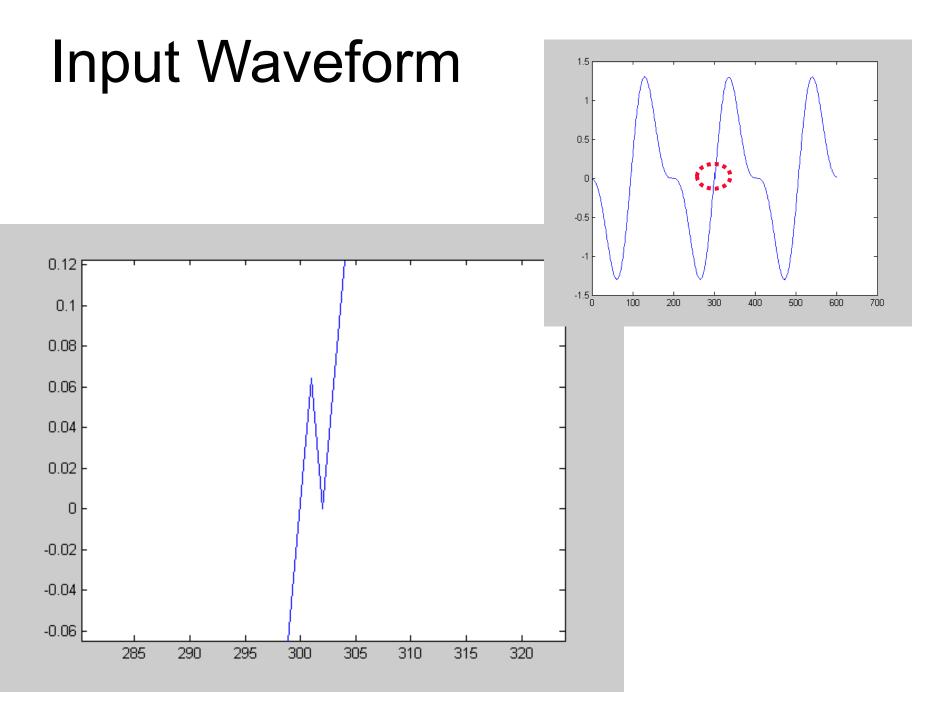
Deviation from hypothesis is .05% of the sampling window



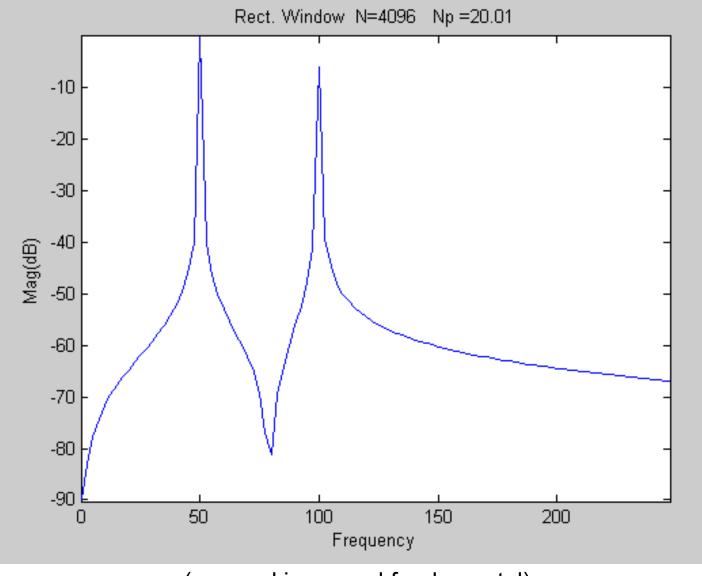








Spectral Response with Non-Coherent Sampling



(zoomed in around fundamental)

Fundamental will appear at position 1+Np = 21

Columns 1 through 7

-89.8679 -83.0583 -77.7239 -74.2607 -71.6830 -69.5948 -67.8044

Columns 8 through 14

-66.2037 -64.7240 -63.3167 -61.9435 -60.5707 -59.1642 -57.6859

Columns 15 through 21

-56.0866 -54.2966 -52.2035 -49.6015 -46.0326 -40.0441 -0.0007

Columns 22 through 28

-40.0162 -46.2516 -50.0399 -52.8973 -55.3185 -57.5543 -59.7864 Columns 29 through 35

-62.2078 -65.1175 -69.1845 -76.9560 -81.1539 -69.6230 -64.0636

kth harmonic will appear at position 1+k•Np

Columns 36 through 42

-59.9172 -56.1859 -52.3380 -47.7624 -40.9389 -6.0401 -39.2033

Observations

- Modest change in sampling window of 0.01 out of 20 periods (.05%) still results in a modest error in both fundamental and harmonic
- More importantly, substantial raise in the computational noise floor !!! (from over -300dB to only -40dB)
- Errors at about the 6-bit level !

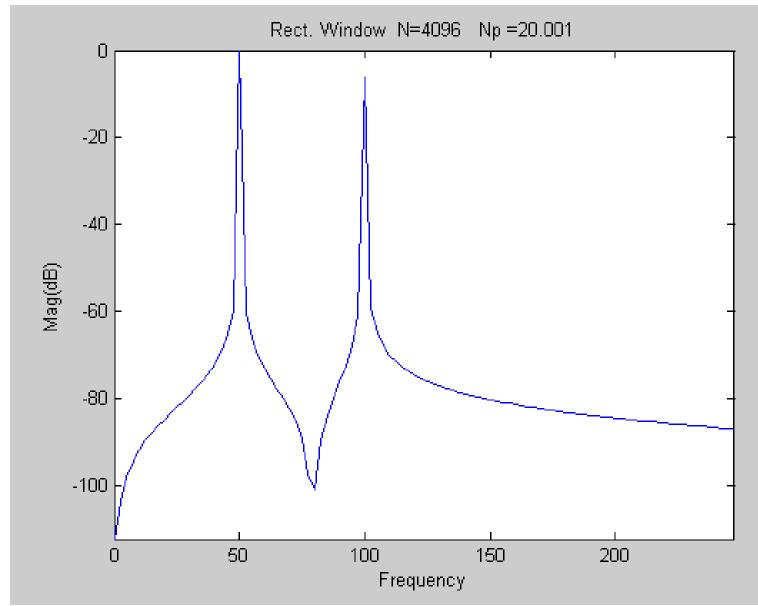
Example

WLOG assume f_{SIG} =50Hz $V_{IN} = sin(\omega t) + 0.5 sin(2\omega t)$ $\omega = 2\pi f_{SIG}$

Consider N_P=20.001 N=4096

Deviation from hypothesis is .005% of the sampling window

Spectral Response with Non-coherent Sampling



(zoomed in around fundamental)

Fundamental will appear at position 1+Np = 21

Columns 1 through 7

-112.2531 -103.4507 -97.8283 -94.3021 -91.7015 -89.6024 -87.8059

Columns 8 through 14

-86.2014 -84.7190 -83.3097 -81.9349 -80.5605 -79.1526 -77.6726

Columns 15 through 21

-76.0714 -74.2787 -72.1818 -69.5735 -65.9919 -59.9650 0.0001

Columns 22 through 28

-60.0947 -66.2917 -70.0681 -72.9207 -75.3402 -77.5767 -79.8121

Columns 29 through 35

-82.2405 -85.1651 -89.2710 -97.2462 -101.0487 -89.5195 -83.9851

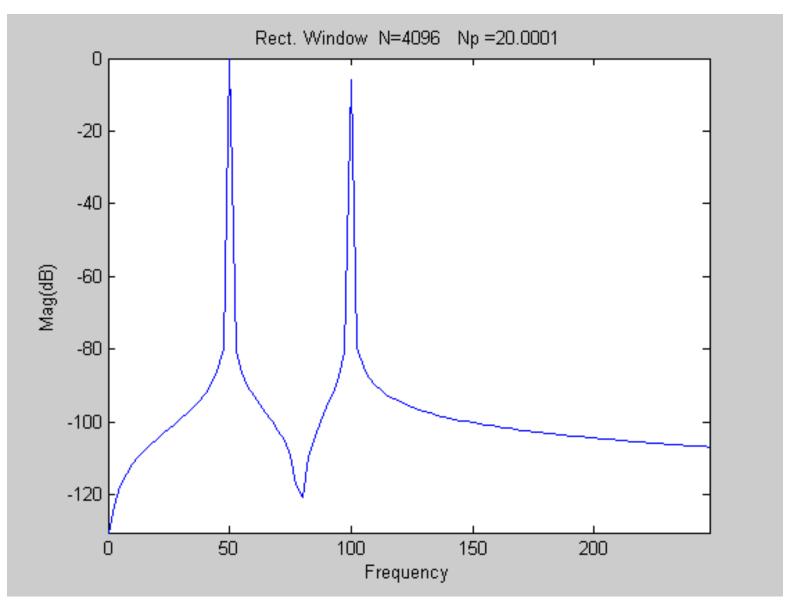
kth harmonic will appear at position 1+k•Np

Columns 36 through 42 -79.8472 -76.1160 -72.2601 -67.6621 -60.7642 -6.0220 -59.3448 Columns 43 through 49 -64.8177 -67.8520 -69.9156 -71.4625 -72.6918 -73.7078 -74.5718 Columns 50 through 56 -75.3225 -75.9857 -76.5796 -77.1173 -77.6087 -78.0613 -78.4809 Columns 57 through 63 -78.8721 -79.2387 -79.5837 -79.9096 -80.2186 -80.5125 -80.7927

Observations

- Modest change in sampling window of 0.001 out of 20 periods (.005%) results in a small error in both fundamental and harmonic
- More importantly, substantial raise in the computational noise floor !!! (from over 300dB to only -60dB)
- Errors at about the 10-bit level !

Spectral Response with Non-coherent sampling



(zoomed in around fundamental)

Fundamental will appear at position 1+Np = 21

Columns 1 through 7

-130.4427 -123.1634 -117.7467 -114.2649 -111.6804 -109.5888 -107.7965

Columns 8 through 14

-106.1944 -104.7137 -103.3055 -101.9314 -100.5575 -99.1499 -97.6702

Columns 15 through 21

-96.0691 -94.2764 -92.1793 -89.5706 -85.9878 -79.9571 0.0000

Columns 22 through 28

-80.1027 -86.2959 -90.0712 -92.9232 -95.3425 -97.5788 -99.8141

Columns 29 through 35

-102.2424 -105.1665 -109.2693 -117.2013 -120.8396 -109.4934 -103.9724

kth harmonic will appear at position 1+k•Np

Columns 36 through 42 -99.8382 -96.1082 -92.2521 -87.6522 -80.7470 -6.0207 -79.3595 Columns 43 through 49 -84.8247 -87.8566 -89.9190 -91.4652 -92.6940 -93.7098 -94.5736 Columns 50 through 56 -95.3241 -95.9872 -96.5810 -97.1187 -97.6100 -98.0625 -98.4821 Columns 57 through 63 -98.8732 -99.2398 -99.5847 -99.9107 -100.2197 -100.5135 -100.7937 Columns 64 through 70

Observations

- Modest change in sampling window of 0.0001 out of 20 periods (.0005%) results in a small error in both fundamental and harmonic
- More importantly, substantial raise in the computational noise floor !!! (from over -300dB to only -80dB)
- Errors at about the 13-bit level !

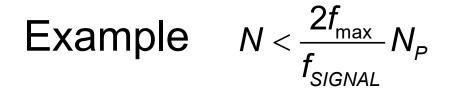
DFT Examples

Recall the theorem that provided for the relationship between the DFT terms and the Fourier Series Coefficients required

1. The sampling window be an integral number of periods

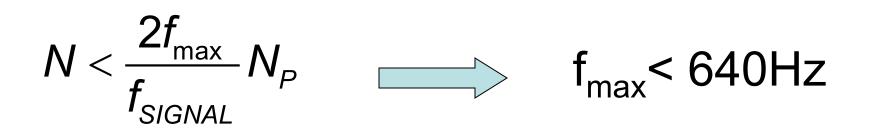
$$N > \frac{2f_{\text{max}}}{f_{\text{SIGNAL}}} N_{P}$$

> 2.



(Not meeting Nyquist sampling rate requirement)

and $N_P=20$ N=512



Example
$$N < \frac{2f_{\text{max}}}{f_{SIGNAL}}N_P$$

(Not meeting Nyquist sampling rate requirement)

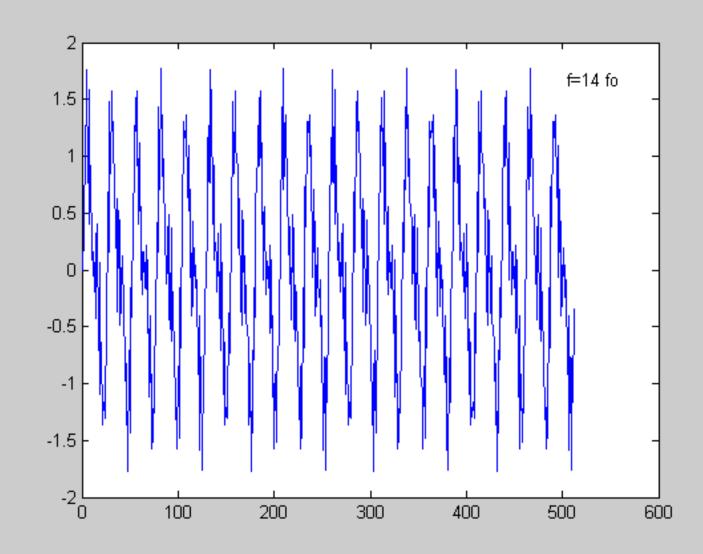
Consider N_P=20 N=512

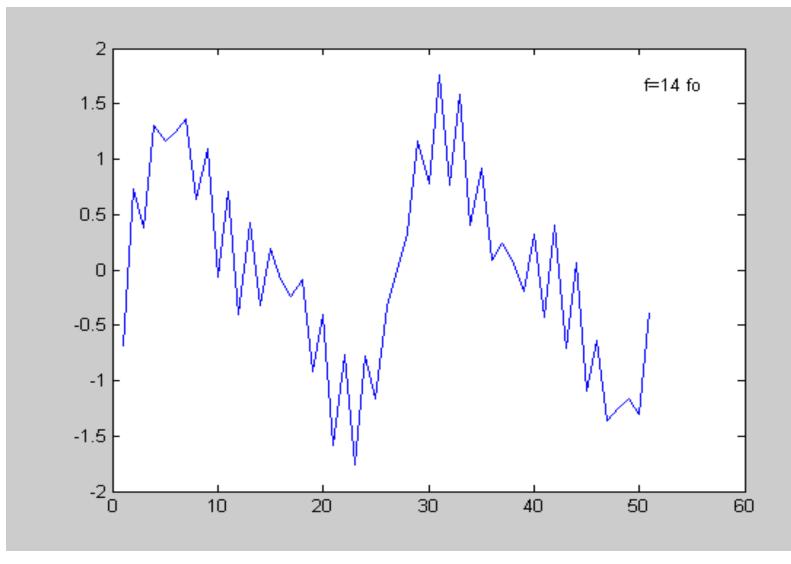
If f_{SIG} =50Hz but an additional input at 700Hz is present

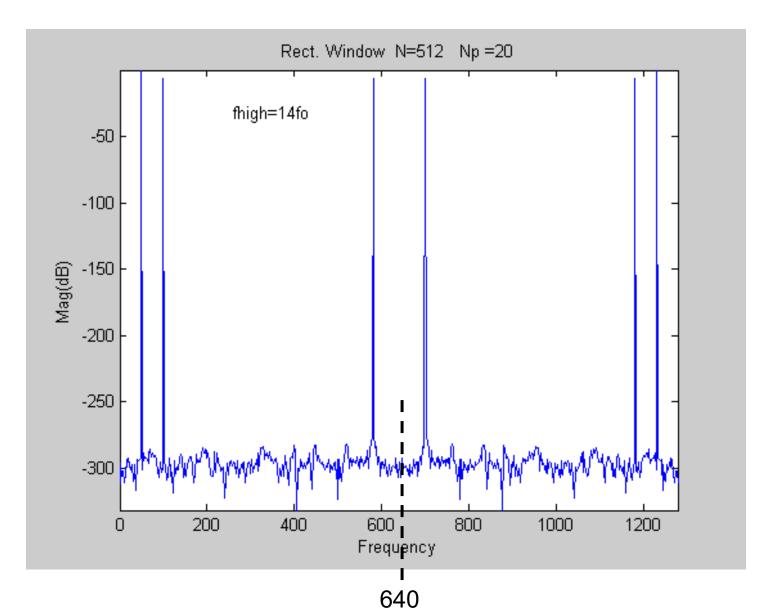
$$N_{P} = \frac{NT_{S}}{T} \quad \leftrightarrow \quad f_{SAMP} = f_{SIGNAL} \frac{N}{N_{P}} \qquad f_{SAMP} = 1.280 \text{KHz}$$
$$V_{IN} = \sin(\omega t) + 0.5 \sin(2\omega t) + 0.5 \sin(14\omega t)$$
$$\omega = 2\pi f_{SIG}$$

(i.e. the component at 700 Hz which violates the band limit requirement – Nyquist rate for the 700 Hz input is 1.4KHz)

Recall $20\log_{10}(0.5)=-6.0205999$







Effects of High-Frequency Spectral Components f_{hiah} =14fo

Columns 1 through 7

-296.9507 -311.9710 -302.4715 -302.1545 -310.8392 -304.5465 -293.9310

Columns 8 through 14

-299.0778 -292.3045 -297.0529 -301.4639 -297.3332 -309.6947 -308.2308

Columns 15 through 21

-297.3710 -316.5113 -293.5661 -294.4045 -293.6881 -292.6872 -0.0000

Columns 22 through 28

-301.6889 -288.4812 -292.5621 -292.5853 -294.1383 -296.4034 -289.5216

Columns 29 through 35

-285.9204 -292.1676 -289.0633 -292.1318 -290.6342 -293.2538 -296.8434

Effects of High-Frequency Spectral Components f_{high}=14fo

Columns 36 through 42

-301.7087 -307.2119 -295.1726 -303.4403 -301.6427 -6.0206 -295.3018

Columns 43 through 49

-298.9215 -309.4829 -306.7363 -293.0808 -300.0882 -306.5530 -302.9962

Columns 50 through 56

-318.4706 -294.8956 -304.4663 -300.8919 -298.7732 -301.2474 -293.3188

Aliased components at
$$f_{alias} = f_{sample} - f_{alias}$$

$$f_{alias} = 25.6f_{sig} - 14f_{sig} = 11.6f_{sig}$$

thus position in sequence =
$$1 + N_p \frac{f_{alias}}{f_{sig}} = 1 + 20 \cdot 11.6 = 233$$

Columns 225 through 231

-296.8883 -292.8175 -295.8882 -286.7494 -300.3477 -284.4253 -282.7639

Columns 232 through 238

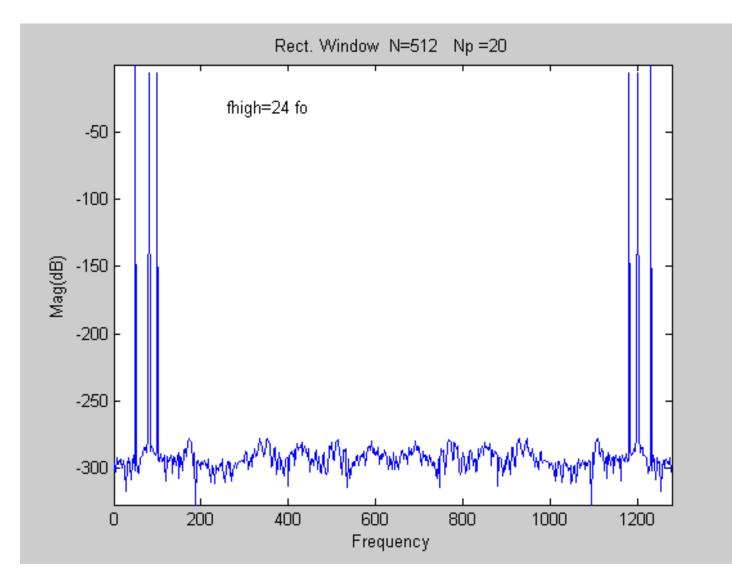
-273.9840 -6.0206 -274.2295 -284.4608 -283.5228 -297.6724 -291.7545

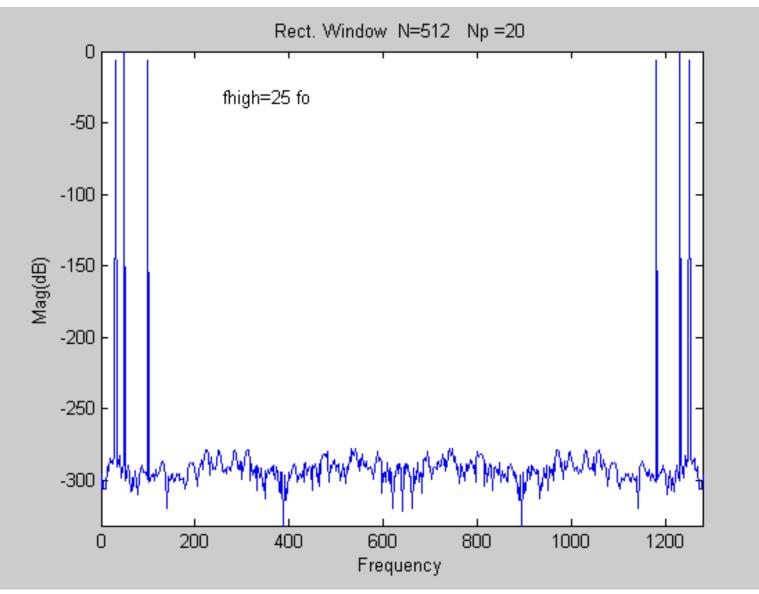
Columns 239 through 245

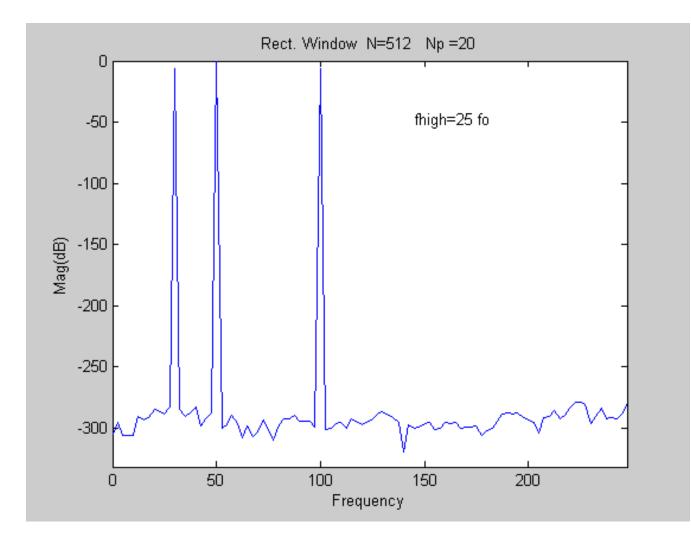
-299.1299 -305.8361 -295.1772 -295.1670 -300.2698 -293.6406 -304.2886

Columns 246 through 252

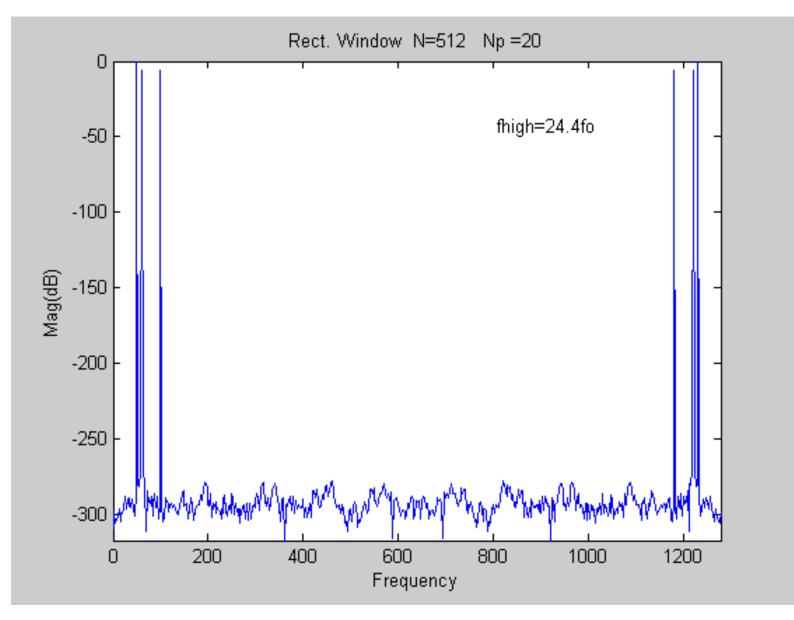
-302.0233 -306.6100 -297.7242 -305.4513 -300.4242 -298.1795 -299.0956

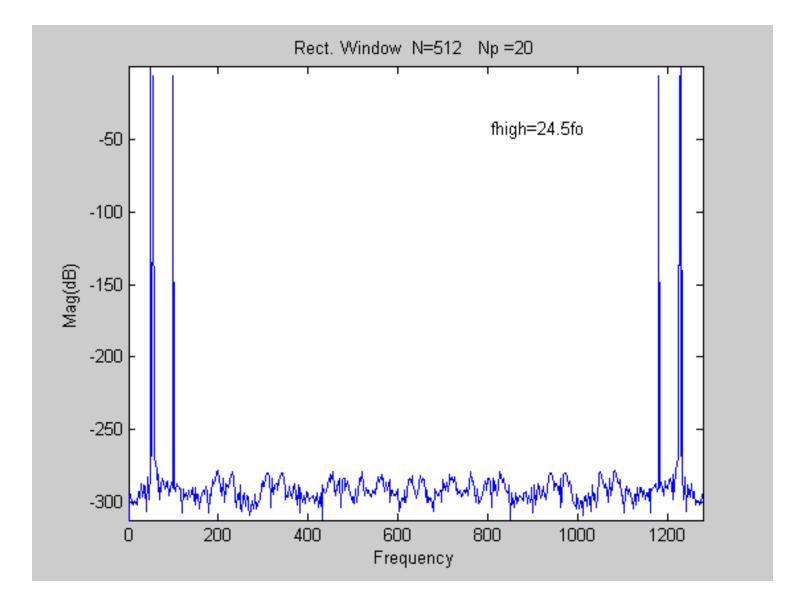






(zoomed in around fundamental)





Observations

- Aliasing will occur if the band-limited part of the hypothesis for using the DFT is not satisfied
- Modest aliasing will cause high frequency components that may or may not appear at a harmonic frequency
- More egregious aliasing can introduce components near or on top of fundamental and lower-order harmonics
- Important to avoid aliasing if the DFT is used for spectral characterization

Review Questions

Q1: How many DFT terms are there if the sample window is of length 4096?

A: 4096

Q2: When the magnitude of the DFT coefficients are plotted, the horizontal axis is an index axis (i.e. dimensionless) but often the index terms are labeled as frequency terms. If the sampling frequency is f_s and N samples are taken, what is the frequency of the first DFT term? What is the frequency of the 2nd DFT term?

A: 0 Hz A: fs/N

Q3: If samples of the time-domain signal are made over exactly 31 periods, which index term corresponds to the fundamental? To the second harmonic?

A: 32nd term A: 63rd term

Q4: What is the difference between the DFT and the FFT?

A: FFT is a computationally efficient method of computing the DFT

Q5: True or False: The DFT terms are real numbers.

A: False We are, however, often interested most in the magnitude of the DFT terms and these are real

Q6: True or False: The magnitude of the DFT terms are symmetric around index number N/2. A: Yes

Considerations for Spectral Characterization

- Tool Validation
- DFT Length and NP
- Importance of Satisfying Hypothesis
 - NP is an integer
 - Band-limited excitation
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Considerations for Spectral Characterization

- Tool Validation
- DFT Length and NP
- Importance of Satisfying Hypothesis
 - NP is an integer
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- Windowing

Are there any strategies to address the problem of requiring precisely an integral number of periods to use the FFT?

Windowing is sometimes used

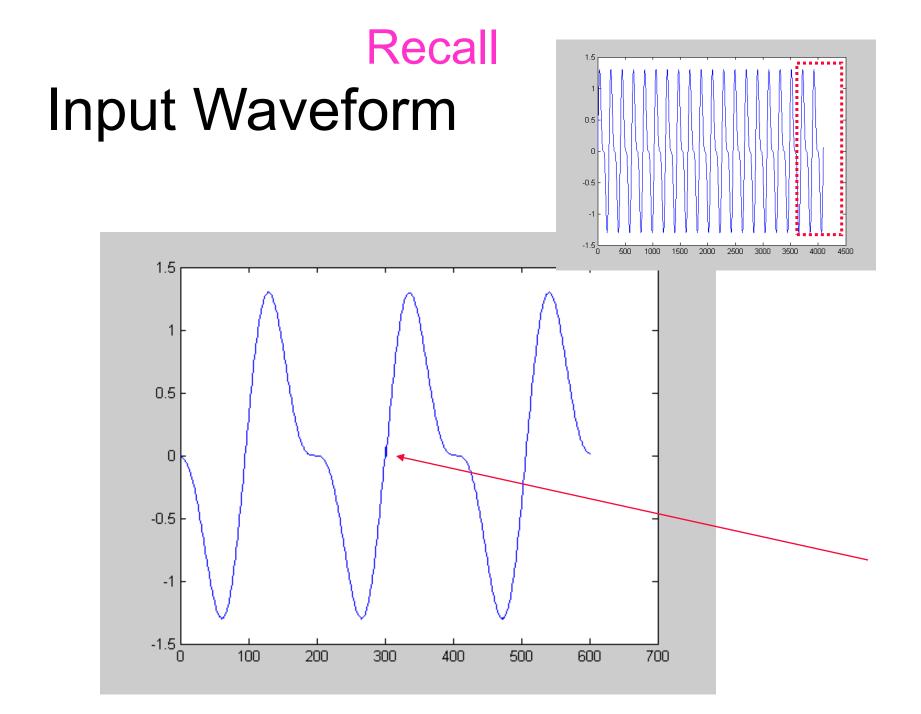
Windowing is sometimes misused

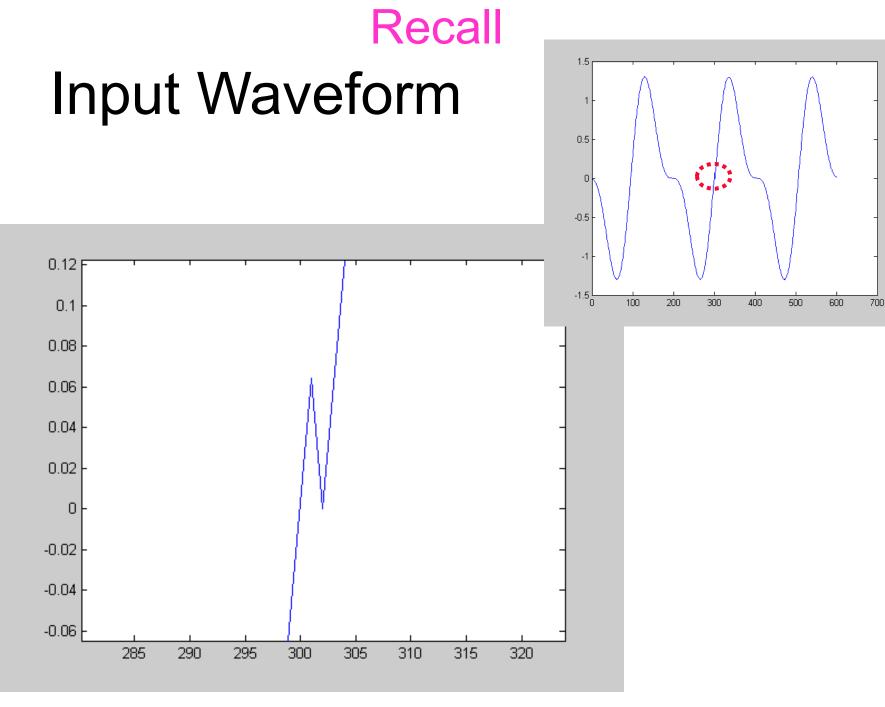
Windowing

Windowing is the weighting of the time domain function to maintain continuity at the end points of the sample window

Well-studied window functions:

- Rectangular (also with appended zeros)
- Triangular
- Hamming
- Hanning
- Blackman





Sometimes termed a boxcar window

Uniform weight

Can append zeros

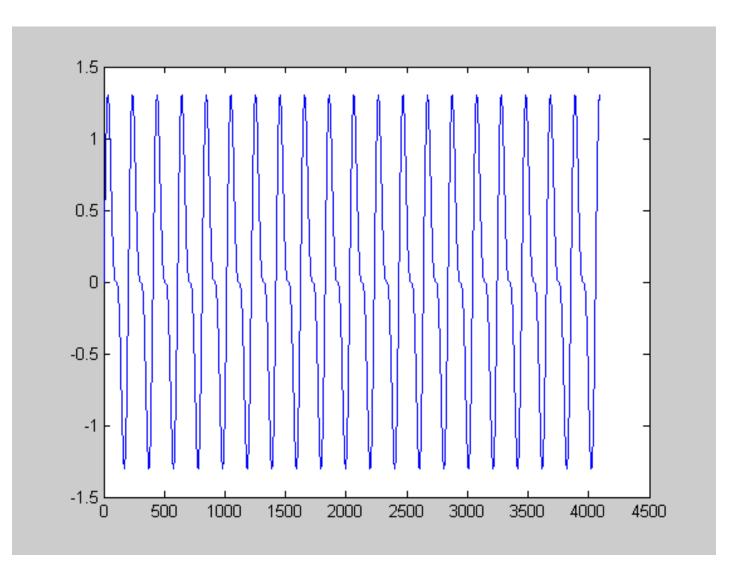
Without appending zeros equivalent to no window

Assume f_{SIG} =50Hz

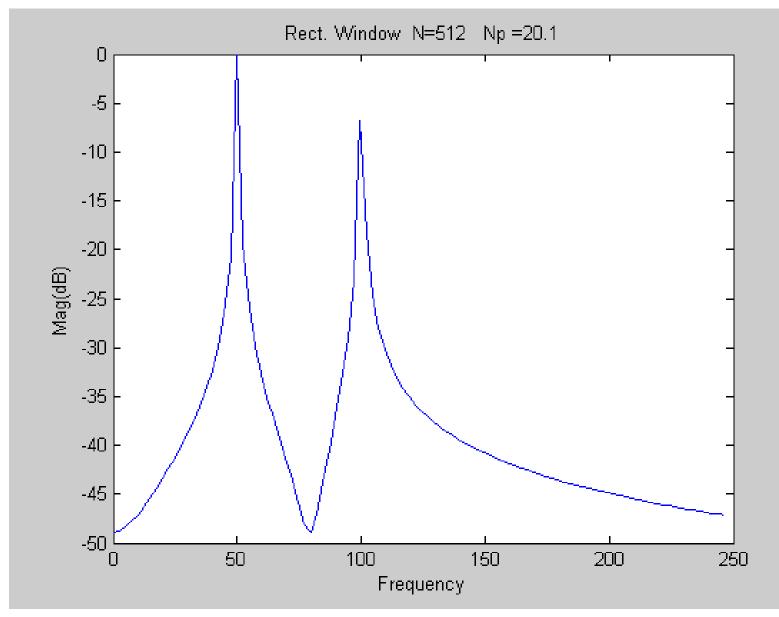
 $V_{IN} = \sin(\omega t) + 0.5 \sin(2\omega t)$

 $\omega = 2\pi f_{SIG}$

Consider N_P =20.1 N=512

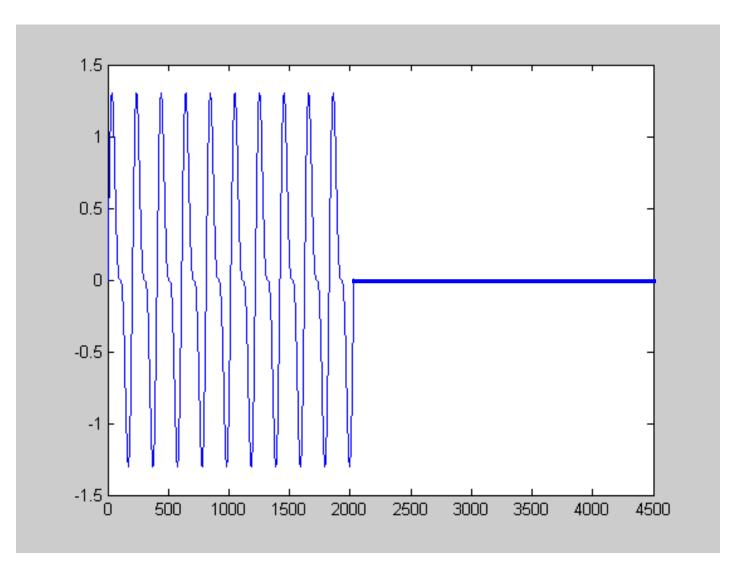


Spectral Response with Non-coherent sampling



(zoomed in around fundamental)

Rectangular Window (with appended zeros)



Columns 1 through 7

-48.8444 -48.7188 -48.3569 -47.7963 -47.0835 -46.2613 -45.3620

Columns 8 through 14

-44.4065 -43.4052 -42.3602 -41.2670 -40.1146 -38.8851 -37.5520

Columns 15 through 21

-36.0756 -34.3940 -32.4043 -29.9158 -26.5087 -20.9064 -0.1352

Columns 22 through 28

-19.3242 -25.9731 -29.8688 -32.7423 -35.1205 -37.2500 -39.2831 Columns 29 through 35

-41.3375 -43.5152 -45.8626 -48.0945 -48.8606 -46.9417 -43.7344

Columns 1 through 7

-48.8444 -48.7188 -48.3569 -47.7963 -47.0835 -46.2613 -45.3620

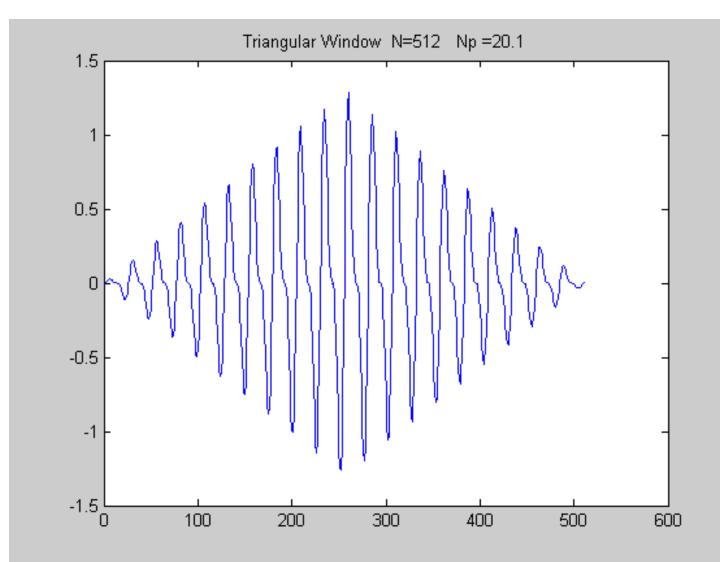
Columns 8 through 14

-44.4065 -43.4052 -42.3602 -41.2670 -40.1146 -38.8851 -37.5520

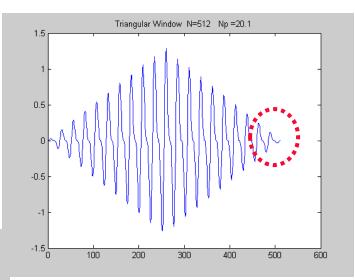
Columns 15 through 21 -36.0756 -34.3940 -32.4043 29.9158 -26.5087 -20.9064 -0.1352 Columns 22 through 28 -19.3242 -25.9731 -29.8688 -32.7423 -35.1205 -37.2500 -39.2831 Columns 29 through 35

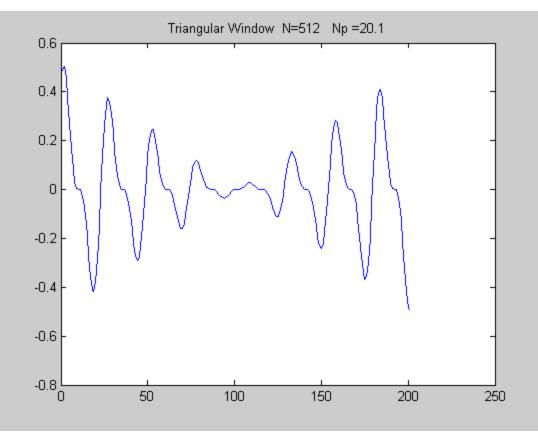
-41.3375 -43.5152 -45.8626 -48.0945 -48.8606 -46.9417 -43.7344 Energy spread over several frequency components

Triangular Window

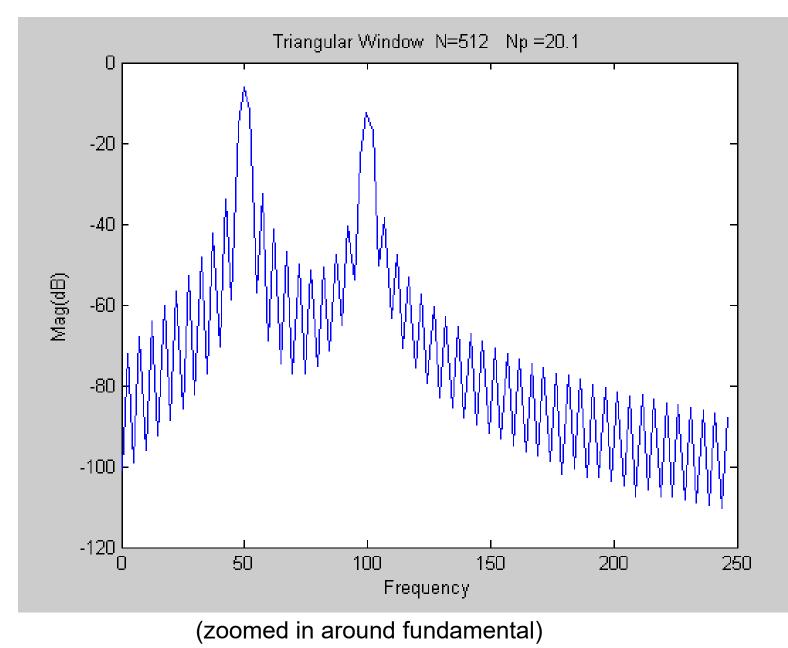


Triangular Window

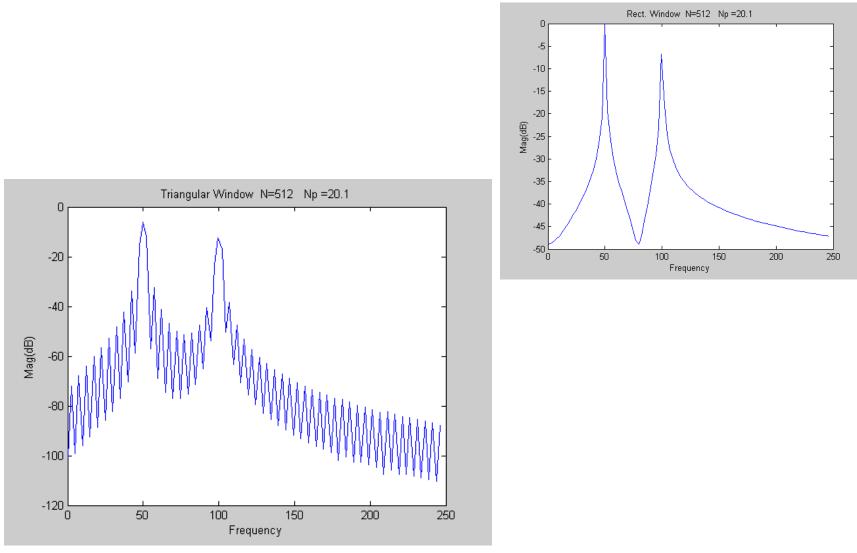




Spectral Response with Non-Coherent Sampling and Windowing



Triangular Window



Triangular Window

Columns 1 through 7

-100.8530 -72.0528 -99.1401 -68.0110 -95.8741 -63.9944 -92.5170

Columns 8 through 14

-60.3216 -88.7000 -56.7717 -85.8679 -52.8256 -82.1689 -48.3134

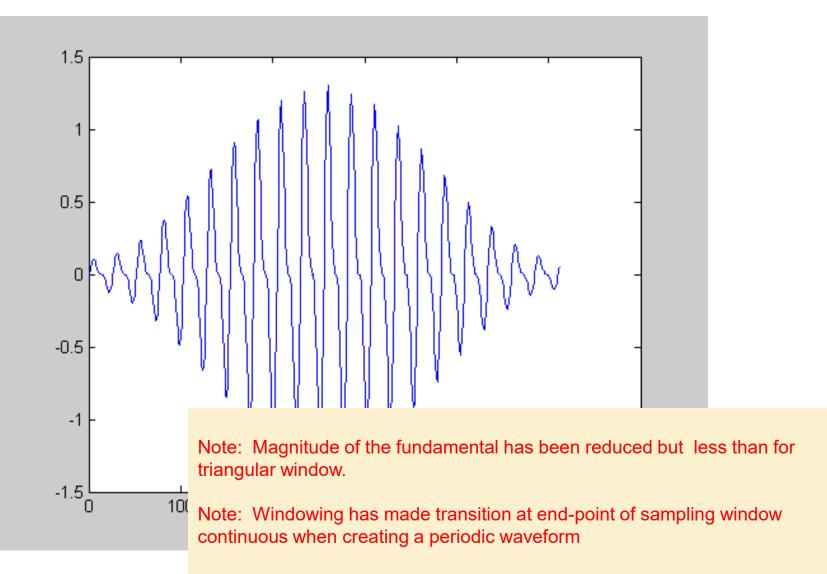
Columns 15 through 21

-77.0594 -42.4247 -70.3128 -33.7318 -58.8762 -15.7333 -6.0918

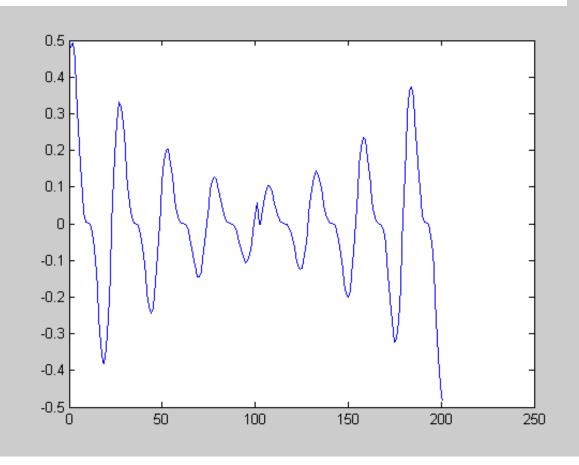
Colu Note: Magnitude of the fundamental has been reduced but the -12. skirting effects have also been reduced.

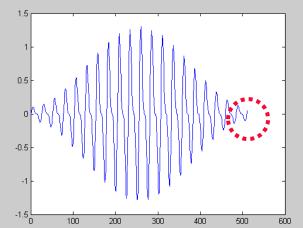
Coll Note: Windowing has reduced energy in the signal but also made transition at end-point of sampling window continuous when creating a periodic waveform

Hamming Window

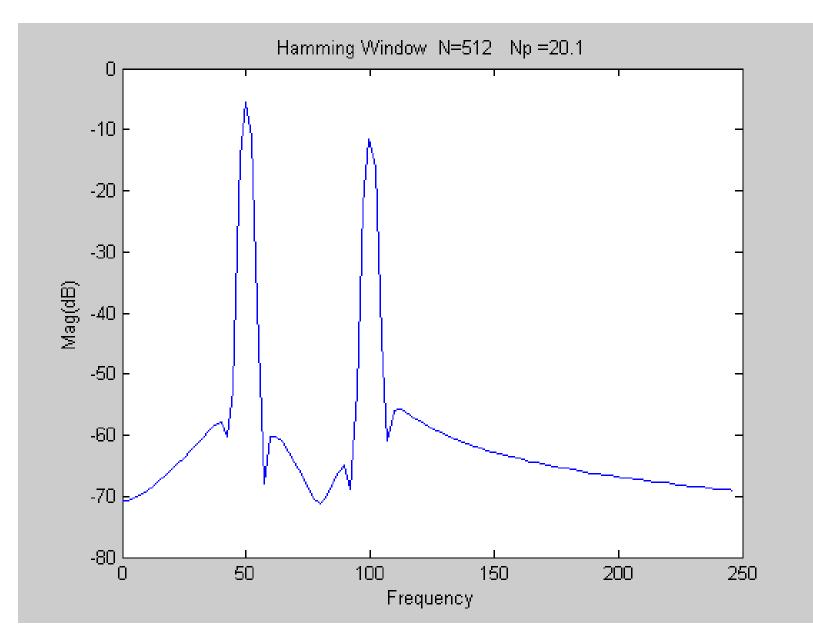


Hamming Window



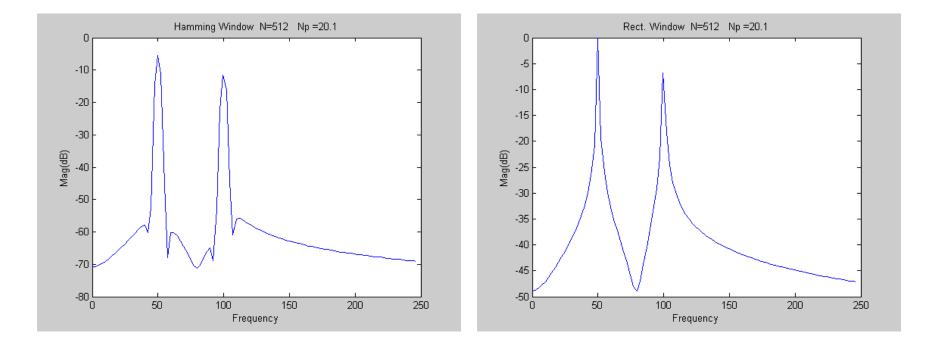


Spectral Response with Non-Coherent Sampling and Windowing



(zoomed in around fundamental)

Comparison with Rectangular Window



Note: Vertical axis are different

Hamming Window

Columns 1 through 7

-70.8278 -70.6955 -70.3703 -69.8555 -69.1502 -68.3632 -67.5133

Columns 8 through 14

-66.5945 -65.6321 -64.6276 -63.6635 -62.6204 -61.5590 -60.4199

Columns 15 through 21

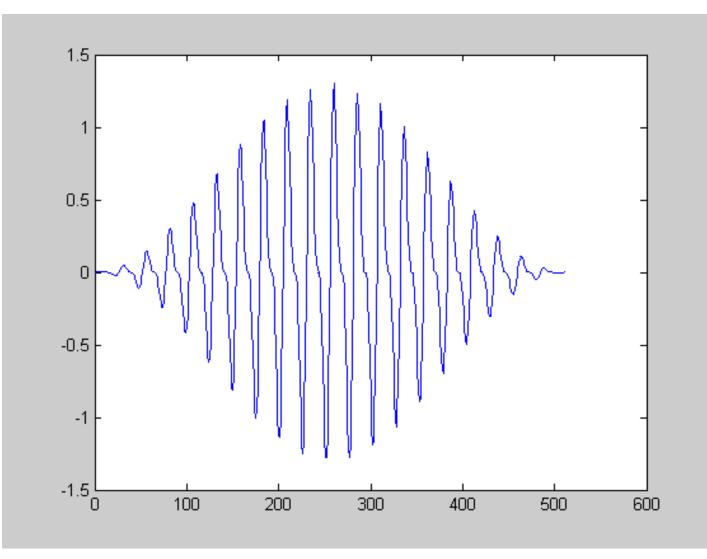
-59.3204 -58.3582 -57.8735 -60.2994 -52.6273 -14.4702 (-5.4343

Columns 22 through 28

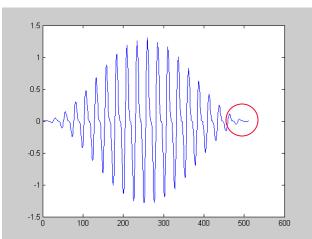
-11.2659 -45.2190 -67.9926 -60.1662 -60.1710 -61.2796 -62.7277 Columns 29 through 35

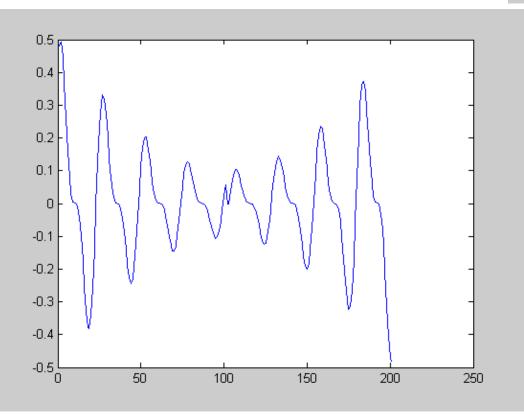
-64.3642 -66.2048 -68.2460 -70.1835 -71.1529 -70.2800 -68.1145

Hanning Window

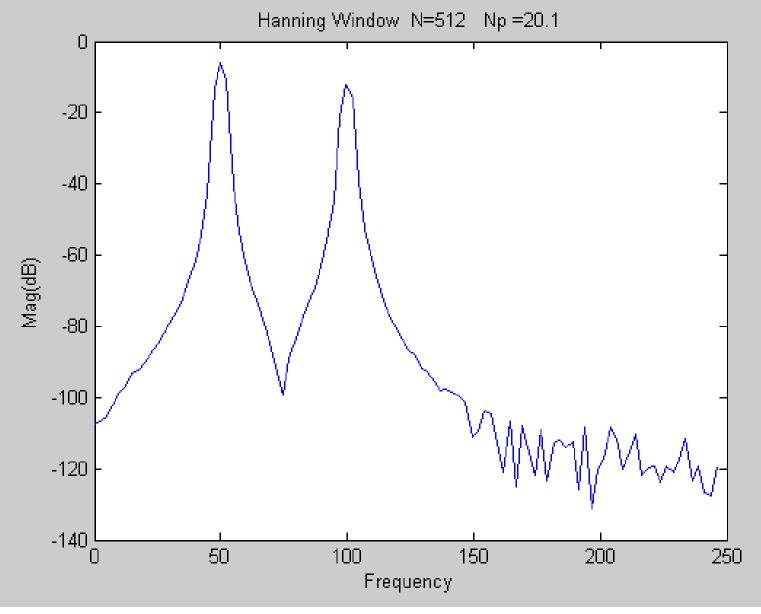


Hanning Window



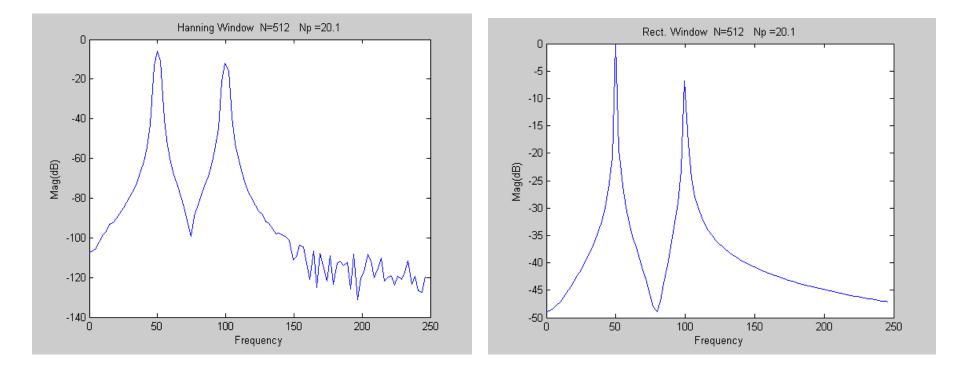


Spectral Response with Non-Coherent Sampling and Windowing



(zoomed in around fundamental)

Comparison with Rectangular Window



Note: Vertical axis are different

Hanning Window

Columns 1 through 7

-107.3123 -106.7939 -105.3421 -101.9488 -98.3043 -96.6522 -93.0343

Columns 8 through 14

-92.4519 -90.4372 -87.7977 -84.9554 -81.8956 -79.3520 -75.8944

Columns 15 through 21

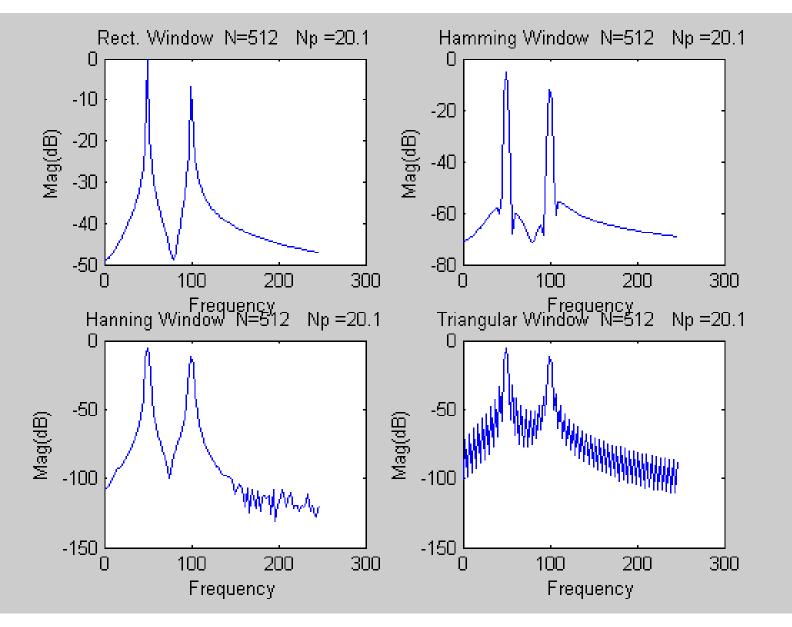
-72.0479 -67.4602 -61.7543 -54.2042 -42.9597 -13.4511 -6.0601

Columns 22 through 28

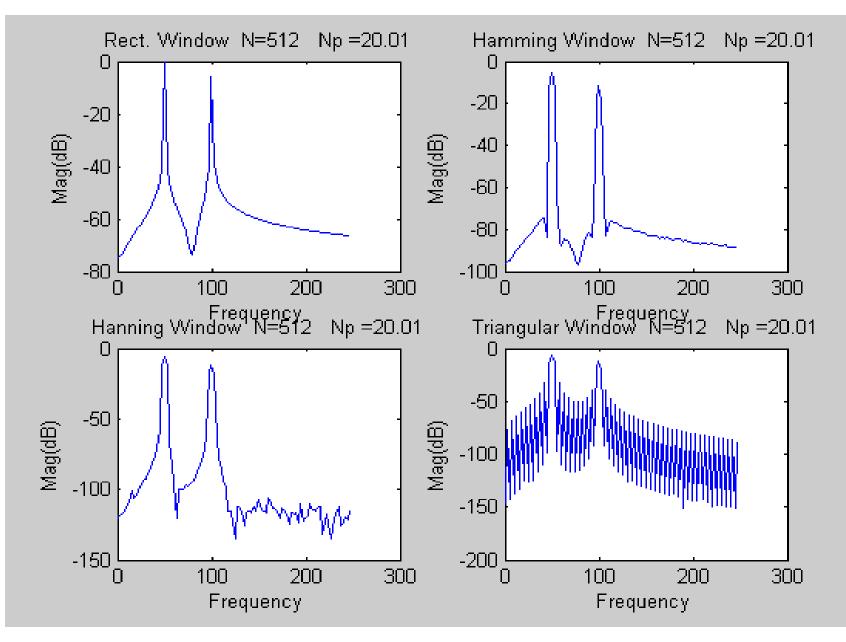
-10.8267 -40.4480 -53.3906 -61.8561 -68.3601 -73.9966 -79.0757 Columns 29 through 35

-84.4318 -92.7280 -99.4046 -89.0799 -83.4211 -78.5955 -73.9788

Comparison of 4 windows



Comparison of 4 windows

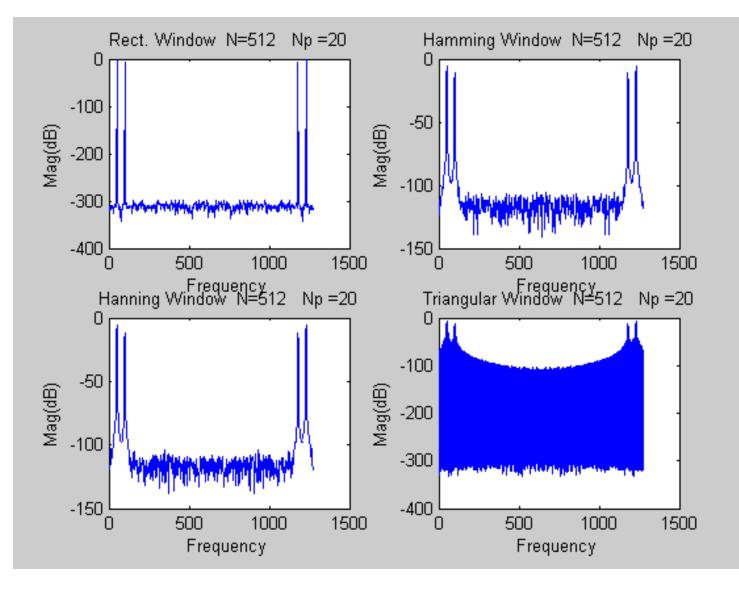


But windows can make things worse too!

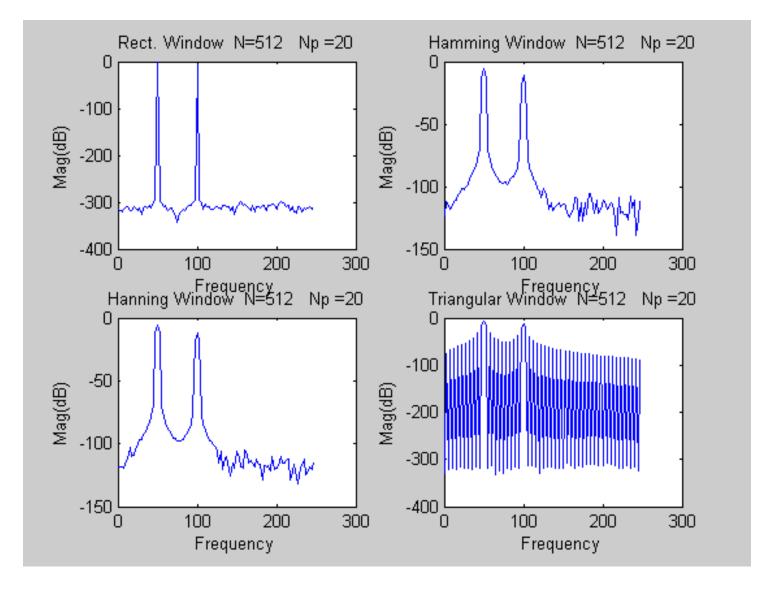
Consider situation where we really do have coherent sampling and a window is applied

fsig1=50Hz fsig2=100Hz N=512 Np=20

Comparison of 4 windows when sampling hypothesis are satisfied



Comparison of 4 windows



But windows can make things worse too!

Consider situation where we really do have coherent sampling and a window is applied

fsig1=50Hz fsig2=100Hz N=512 Np=20

And we do not really know how much worse thing can be!

Be careful about interpreting results obtained by using windowing to mitigate the non-coherent sampling problem !

Remember the hypothesis of the theorem relating the DFT, which is easy to calculate, to the Fourier Series coefficients!

Preliminary Observations about Windows

- Provide separation of spectral components
- Energy can be accumulated around spectral components
- Simple to apply
- Some windows work much better than others

But – windows do not provide dramatic improvement and can significantly degrade performance if sampling hypothesis are met

Issues of Concern for Spectral Analysis

An integral number of periods is critical for spectral analysis

Not easy to satisfy this requirement in the laboratory

Windowing can help but can hurt as well

Out of band energy can be reflected back into bands of interest

Characterization of CAD tool environment is essential

Spectral Characterization of high-resolution data converters requires particularly critical consideration to avoid simulations or measurements from masking real performance

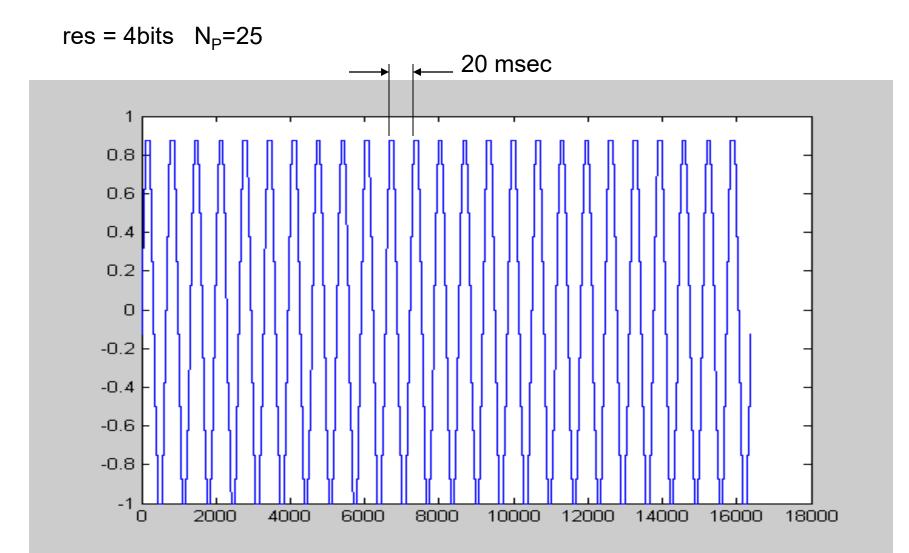
Spectral Characterization of Data Converters

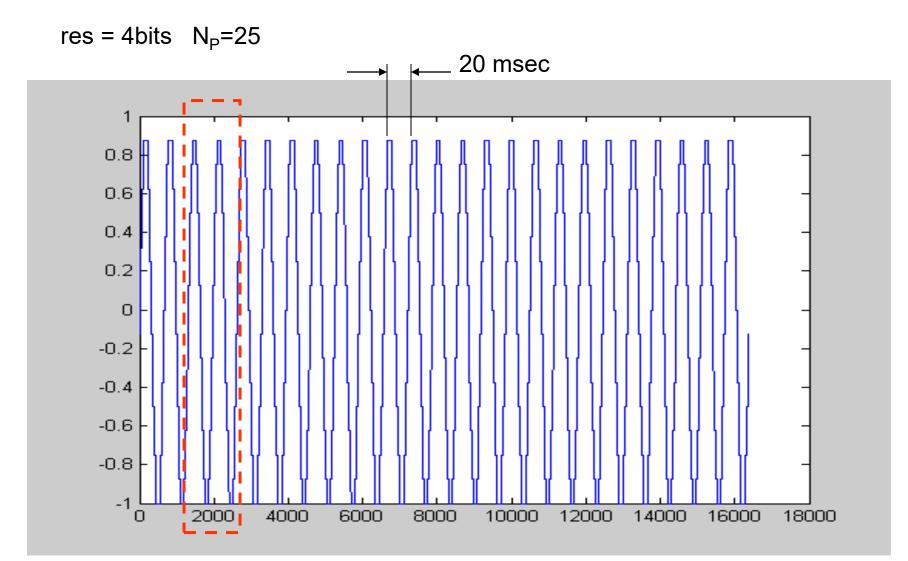
- Distortion Analysis
- → Time Quantization Effects
 - of DACs
 - of ADCs
 - Amplitude Quantization Effects
 - of DACs
 - of ADCs

Quantization Effects on Spectral Performance and Noise Floor in DFT

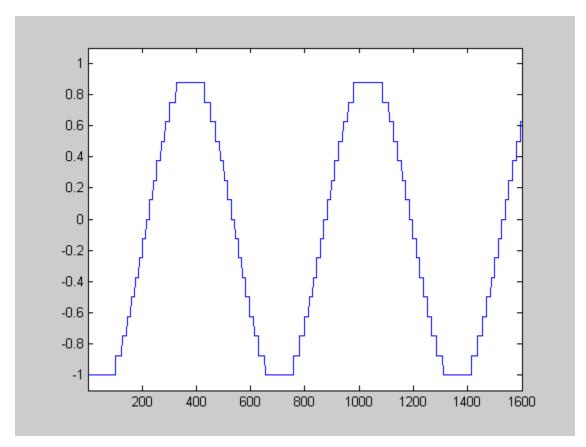
- Assume the effective clock rate (for either an ADC or a DAC) is arbitrarily fast
- Without Loss of Generality it will be assumed that f_{SIG}=50Hz
- Index on DFT will be listed in terms of frequency (rather than index number)

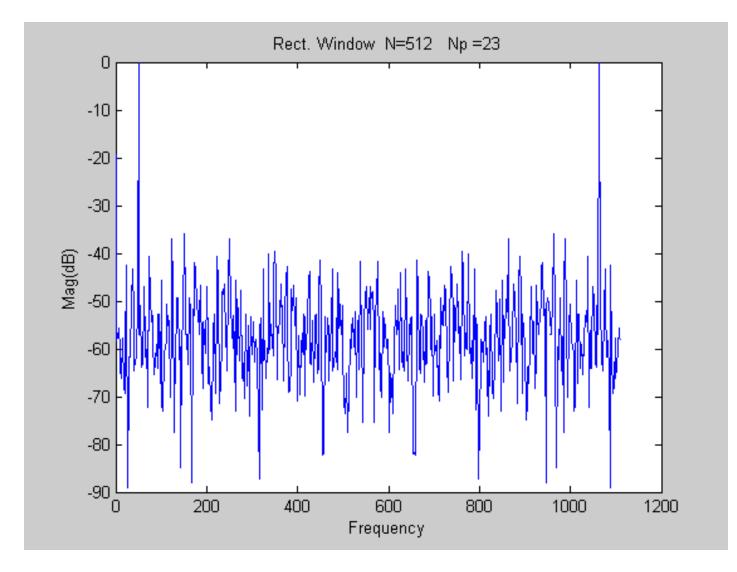
Matlab File: afft_Quantization.m

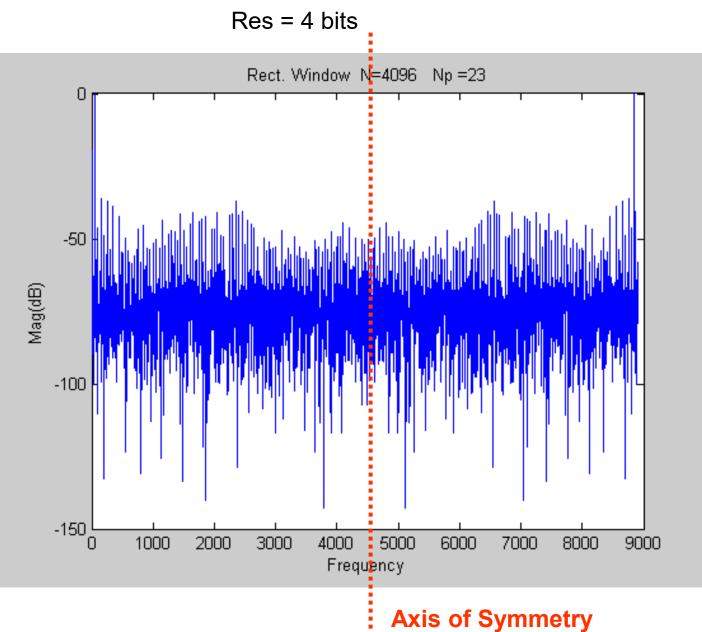




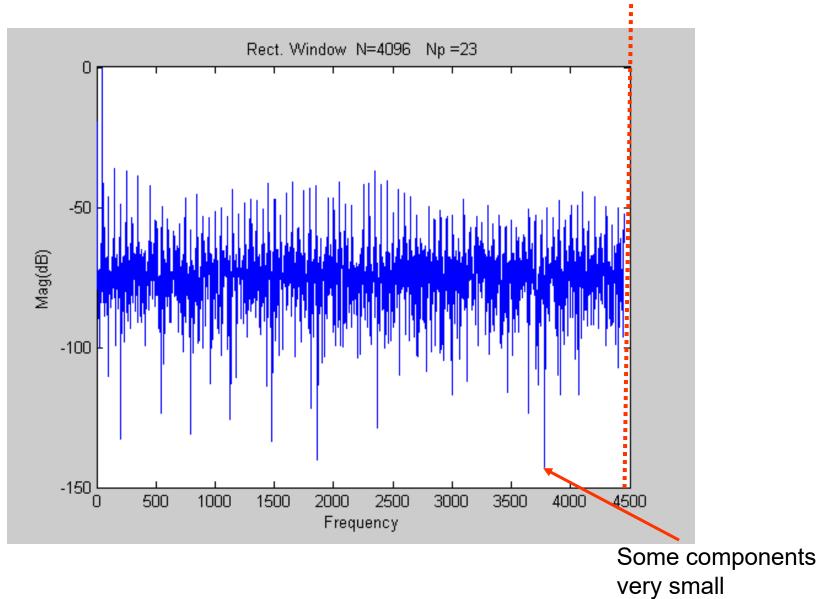
res = 4bits

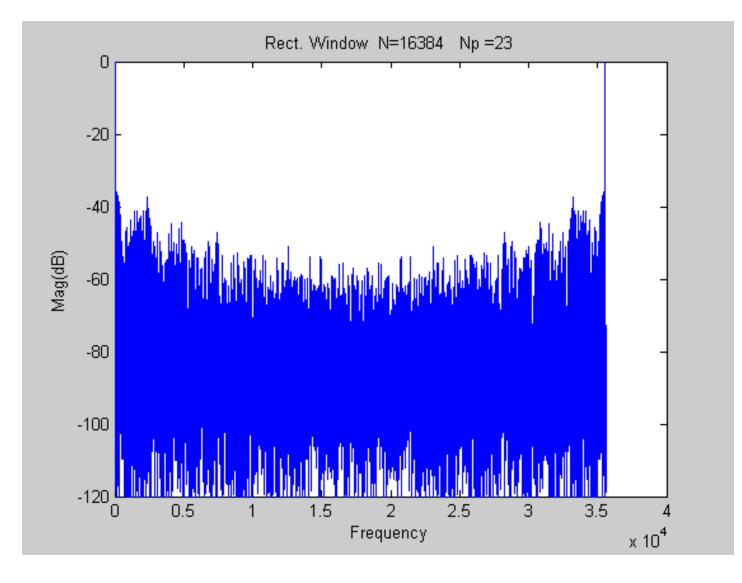


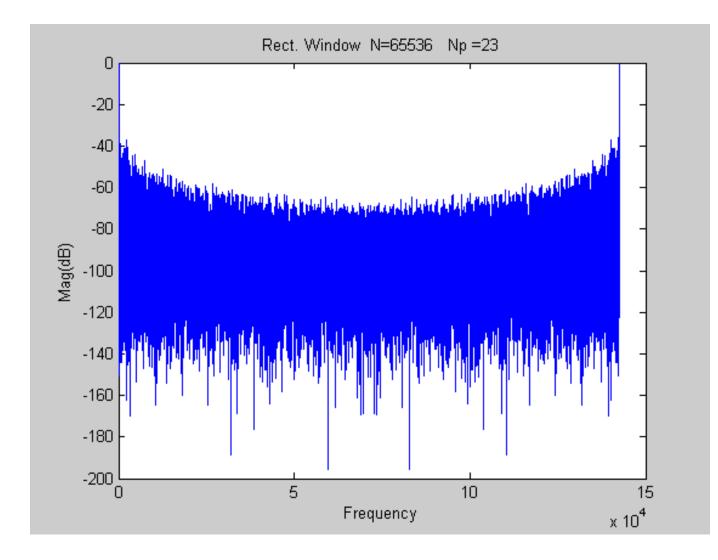


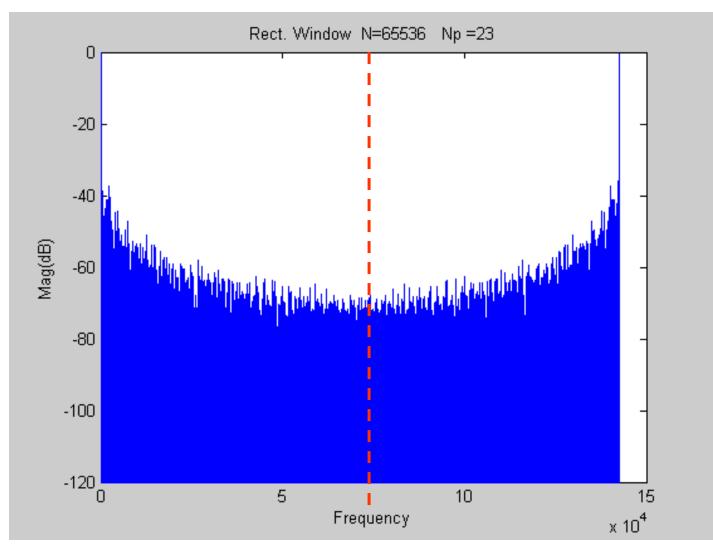


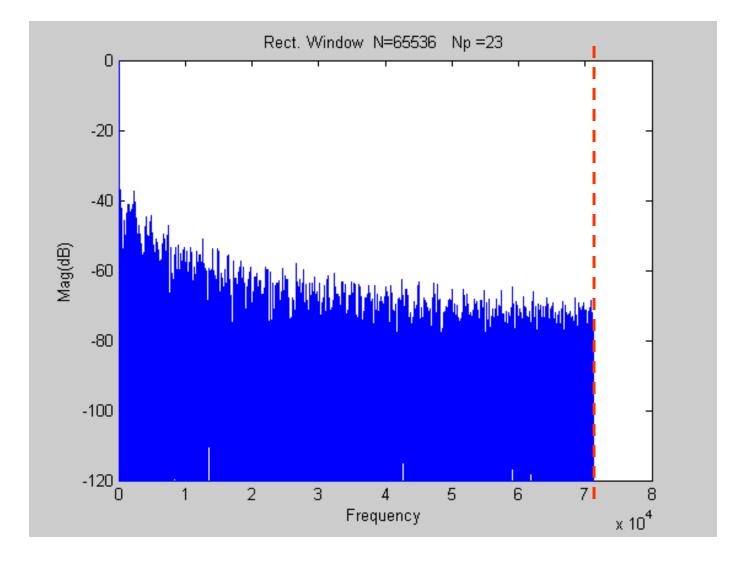
Res = 4 bits

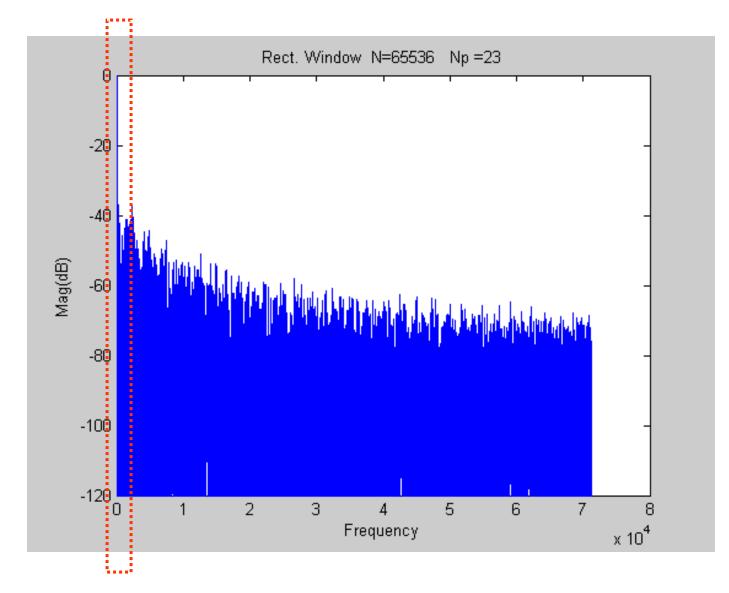


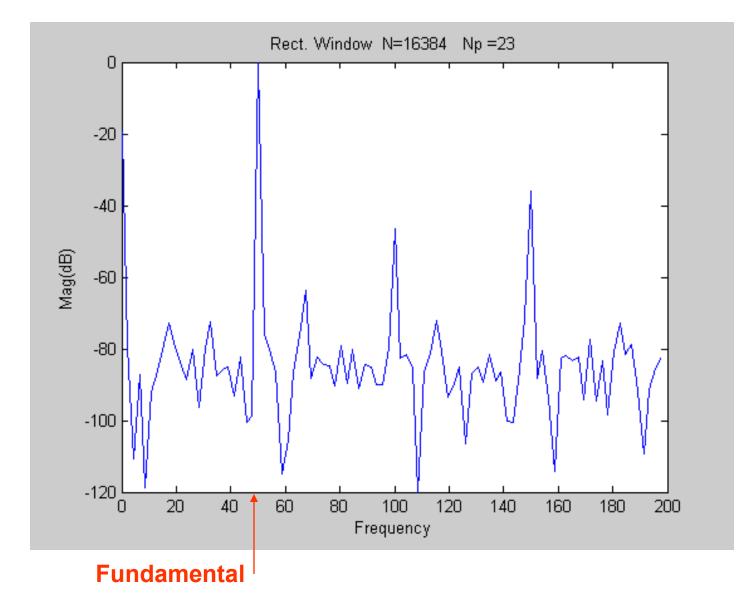




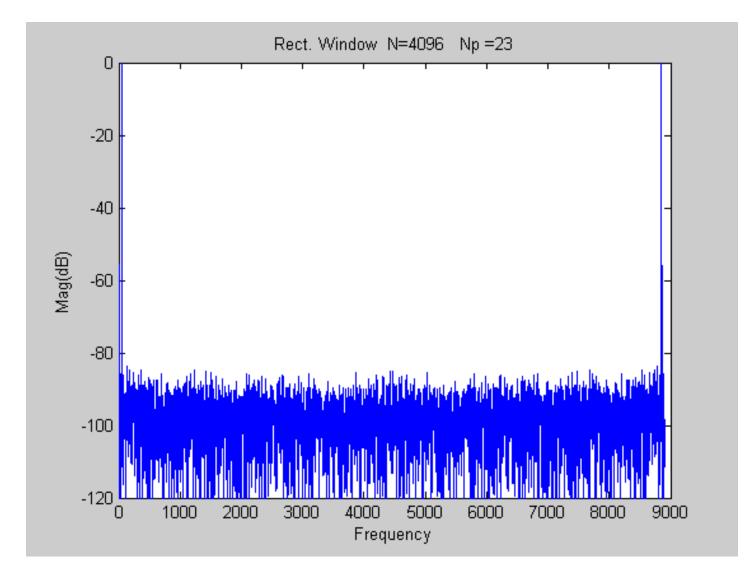


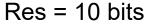


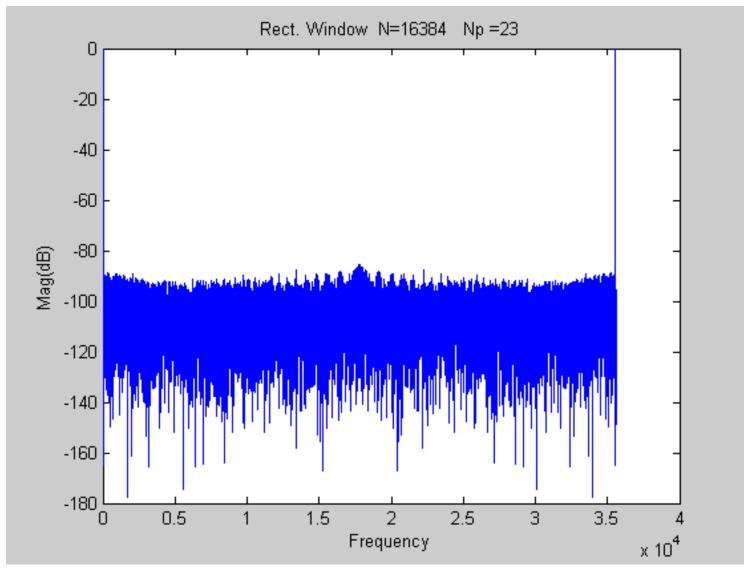




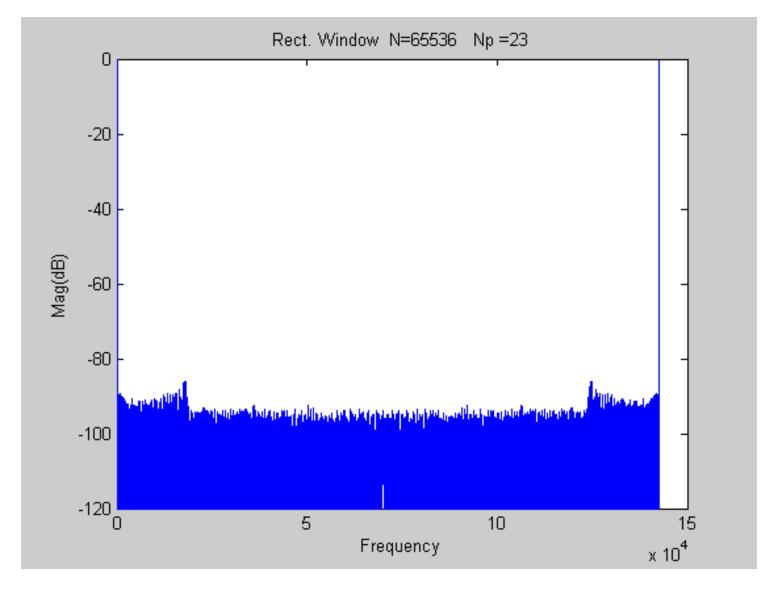
Quantization Effects Res = 10 bits



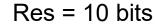


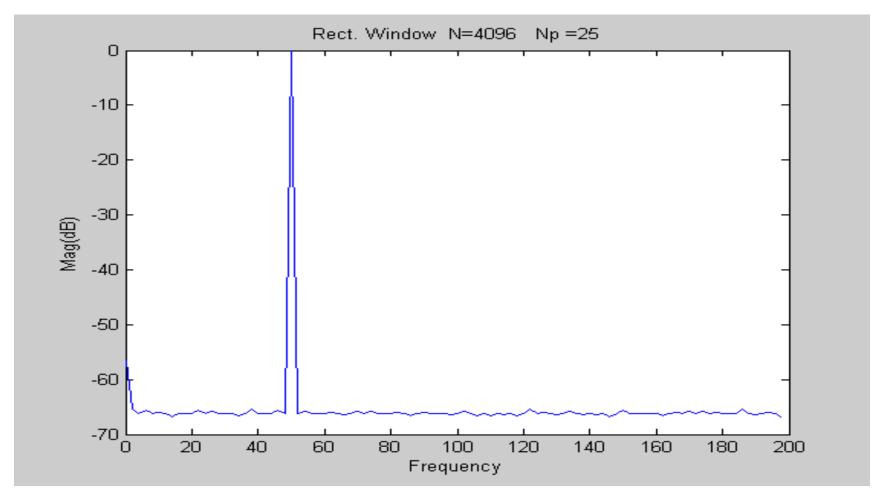


Res = 10 bits



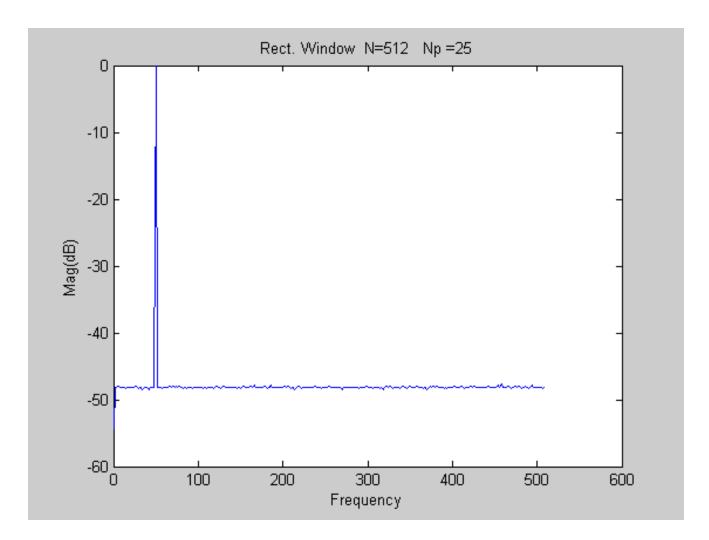
With Vin=2v pp





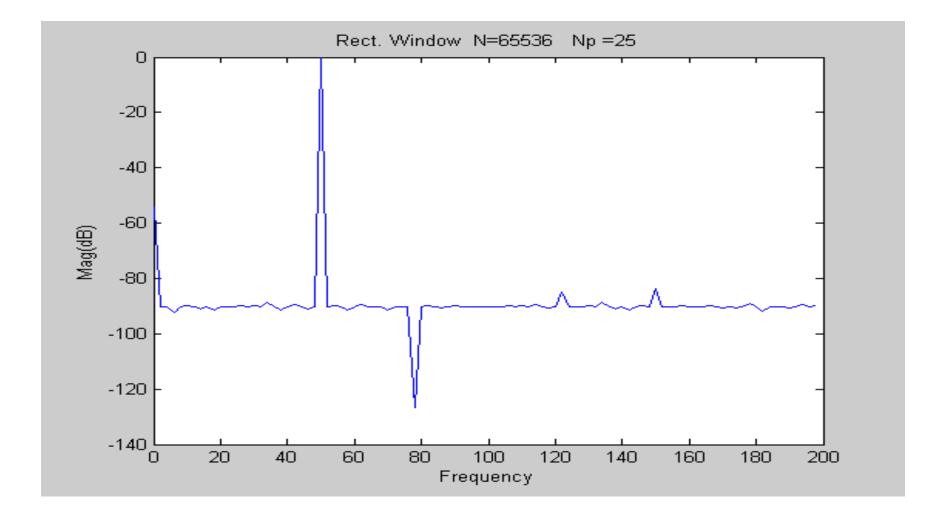
Quantization Effects

Res = 10 bits



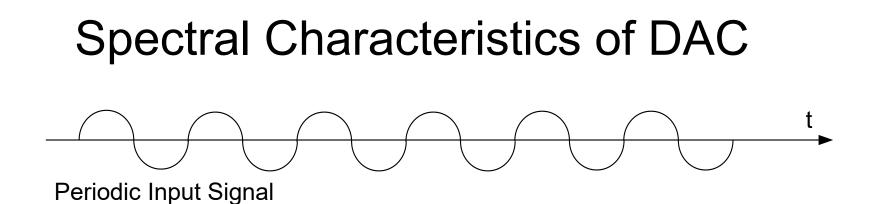
Quantization Effects

Res = 10 bits

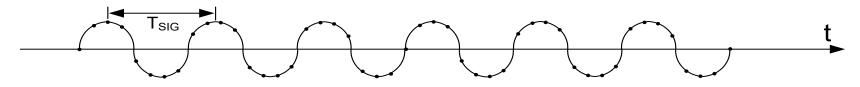


Spectral Characterization of Data Converters

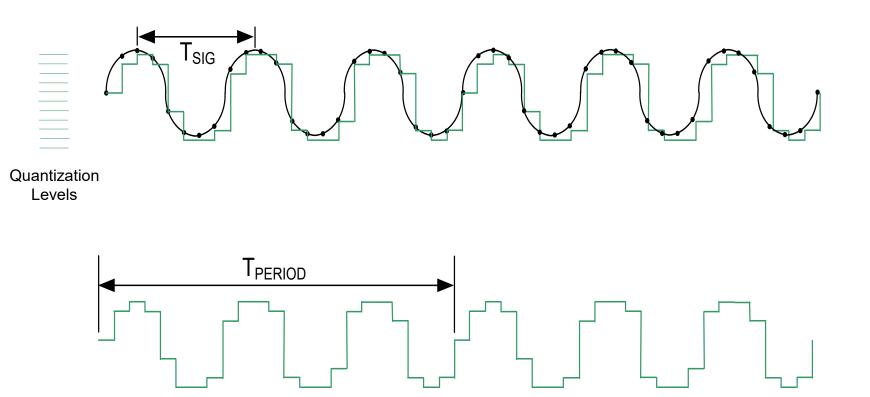
- Distortion Analysis
- → Time Quantization Effects
 - of DACs
 - of ADCs
 - Amplitude Quantization Effects
 - of DACs
 - of ADCs



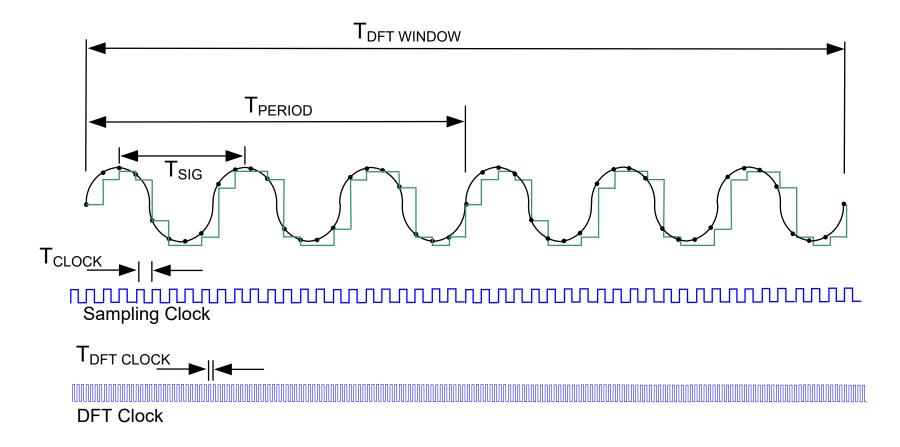
Sampling Clock

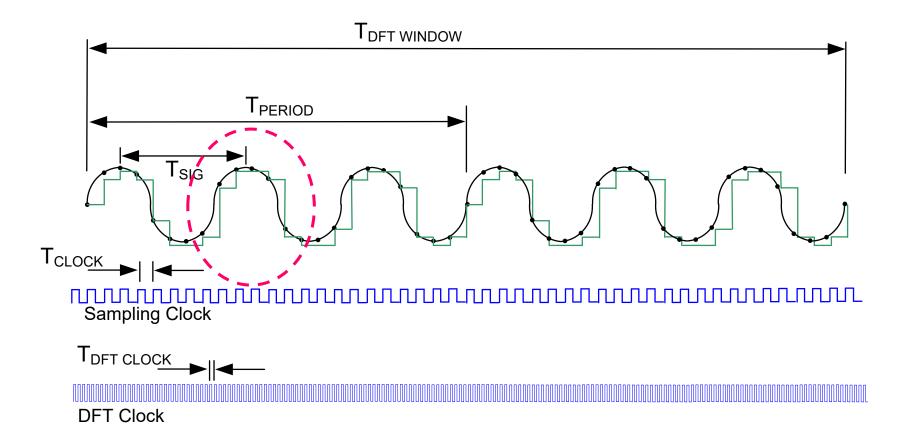


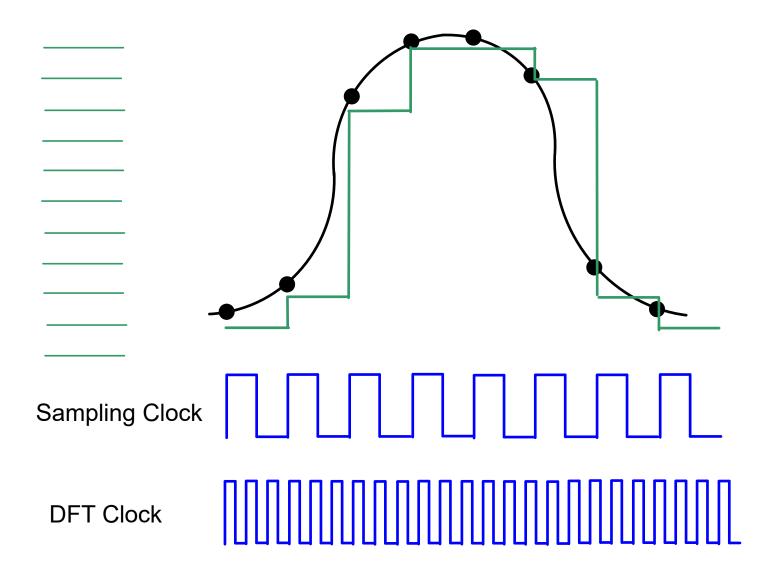
Sampled Input Signal (showing time points where samples taken)

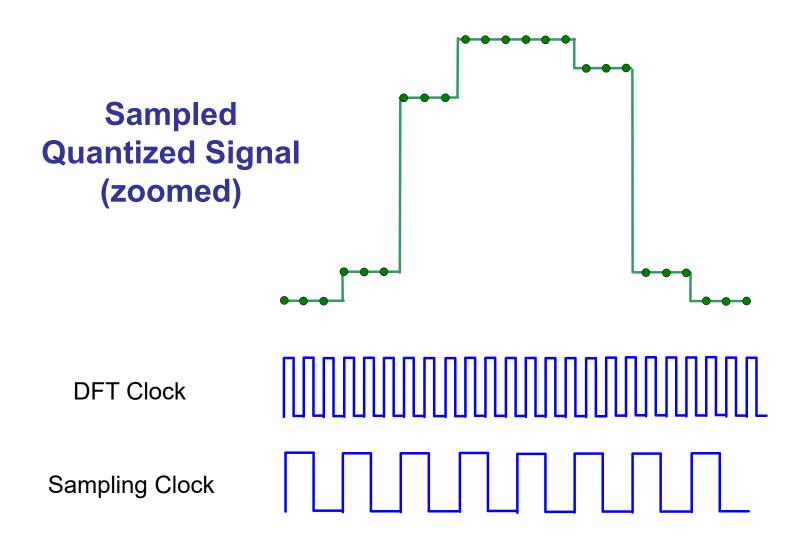


Quantized Sampled Input Signal (with zero-order sample and hold)

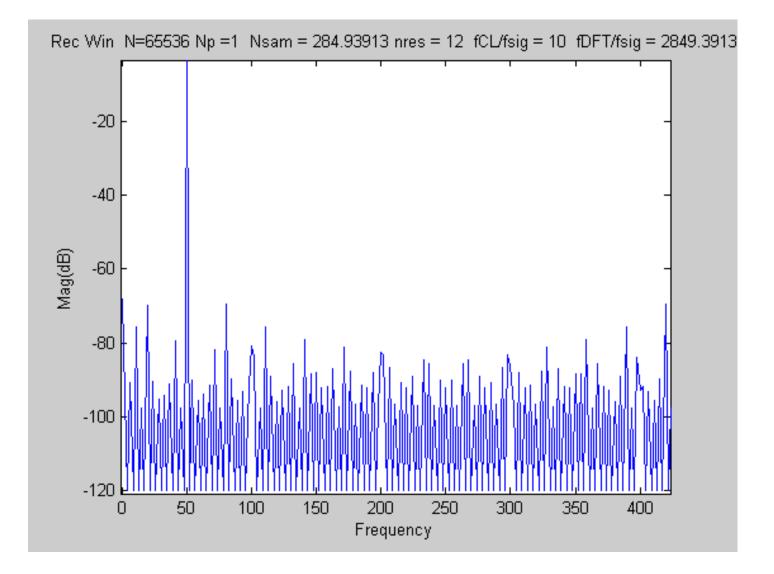








DFT Simulation from Matlab



Summary of time and amplitude quantization assessment

Time and amplitude quantization do not introduce <u>harmonic</u> distortion

Time and amplitude quantization do increase the noise floor



Stay Safe and Stay Healthy !

End of Lecture 29